

### Adv

- ① High sensitivity & selectivity
- ② High adjacent channel rejection
- ③ No variation in B.W.

### Image signal and image signal rejection

→ Superhetrodyne receiver suffers from a major drawback known as image freq problem.

→ Image signal is a signal whose freq. is <sup>as</sup> higher with  $f_o$  as the  $f_{dc}$  is smaller than  $f_o$ .

If  $f_o \rightarrow$  local osc freq.  $f_{dc} \rightarrow$  desired signal freq.  
 $f_i \rightarrow$  intermediate freq.

two,

$$f_o - f_{dc} = f_i \quad \text{--- (1)}$$

$f_{dc}$  is lesser than  $f_o$  with an amount  $f_i$

By definition of image signal

$$f_{im} = f_o + f_i \quad \text{--- (2)}$$

$f_{im} \rightarrow$  image freq.

$$= f_i + f_{dc} + f_i$$

$$= f_{dc} + 2f_i \quad \text{--- (3)}$$

from this eqn it is clear that image signal is  $2f_i$  higher than with desired signal

\* If this signal is reached to antenna mixer by antenna then it will produce same intermediate freq  $f_i$  which will be produced by desired signal  $f_{dc}$ .

$$f_i = f_o - f_{dc}$$

If produced by  $f_{dc}$

$$f_i = f_{im} - f_o$$

If produced by image freq.

$$f_i = f_{im} - f_o$$

$$= f_{dc} + 2f_i - f_o$$

$$= f_{dc} + 2(f_o - f_{dc}) - f_o$$

$$= f_{dc} + 2f_o - 2f_{dc} - f_o$$

$$= f_o - f_{dc} \quad \text{--- (4)}$$

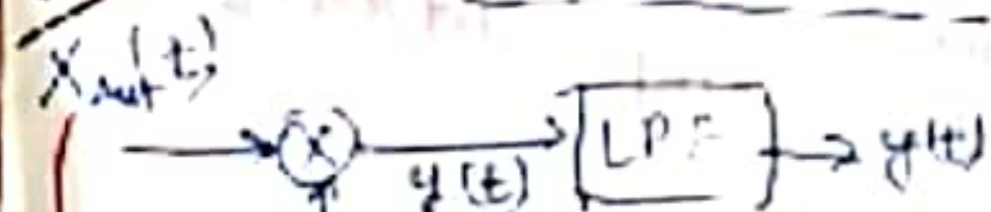
Acc to eqn (1) & eqn (4) desired signal and image signal produce same IF which will further amplify by IF amp and interfere with the signal. so the image signal must be rejected. which depends on selectivity

$\alpha = \sqrt{1 + Q^2 \gamma^2} \Rightarrow$  Image freq. rejection ratio where  $\rho = \frac{f_{im}}{f_{dc}} - \frac{f_{dc}}{f_{im}}$

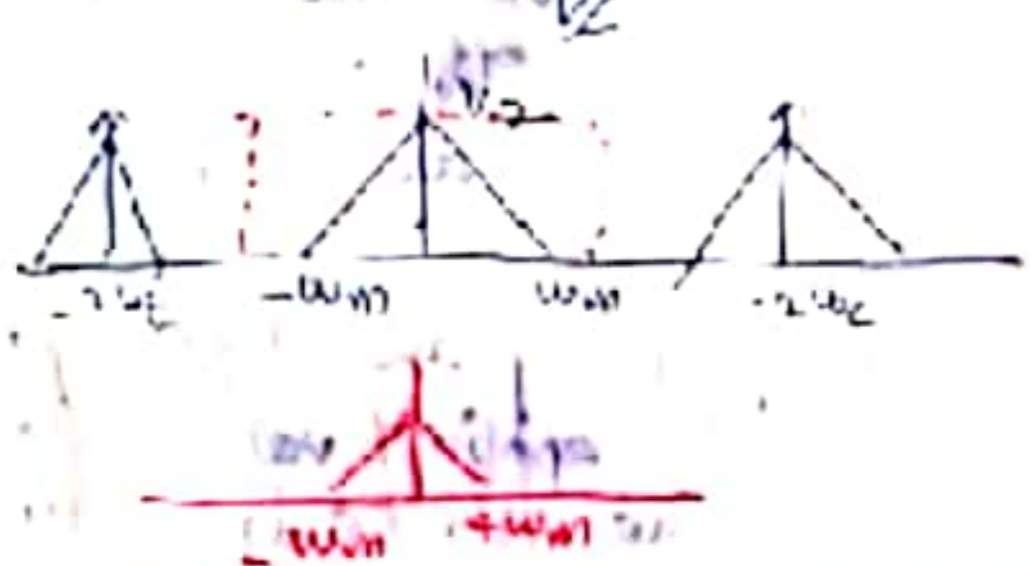
# Demodulation (AM)

## Synchronous Demodulation

DSB-C



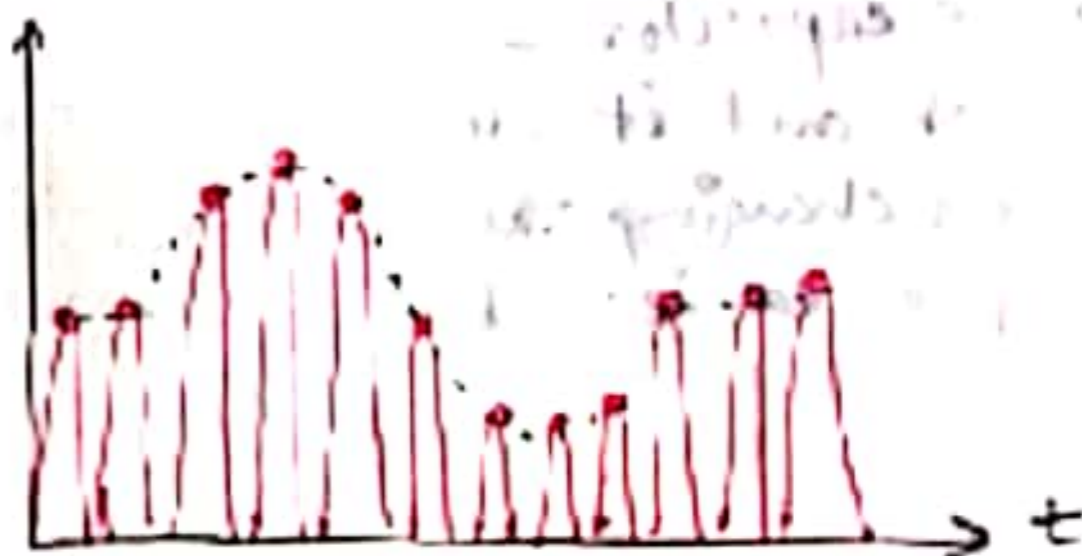
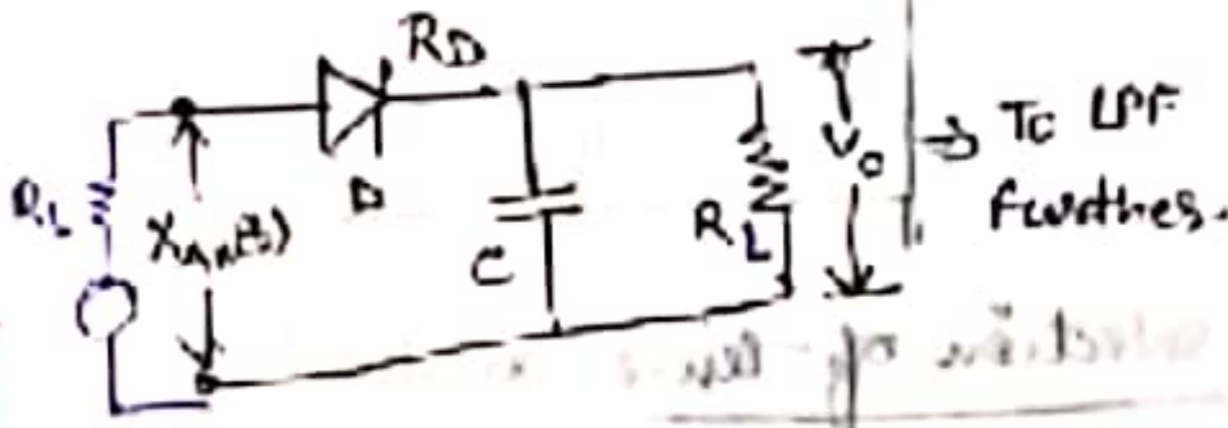
$(A_c + m(t)) \cos wt$   
 $(A_c + m(t)) \cos wt$   
 $= (A_c + m(t)) \left( \frac{1 + \cos 2wt}{2} \right)$   
 $= \frac{A_c}{2} + \frac{A_c}{2} \cos 2wt + \frac{m(t)}{2} + \frac{m(t)}{2} \cos 2wt$



## Asynchronous Demodulation

### Envelope Detector

→ Also called Diode Detector



- In the first half cycle of the ip sig, the diode is forward biased and the cap<sup>r</sup> charges up rapidly to the peak of the ip signal.
- As soon as cap<sup>r</sup> charges to the peak value, the diode stops conducting. The cap<sup>r</sup> will discharge through R between the positive peaks.
- When ip sig falls below the peak value, the diode becomes reverse biased and the cap<sup>r</sup> discharges slowly through the load resistor.
- This discharging process continues until the next positive half cycle, when the ip sig becomes greater than the voltage across the cap<sup>r</sup>, the diode conducts again and process is repeated.

DSB-SC

$$y_1(t) = A_c m(t) \left[ \frac{1 + \cos 2wt}{2} \right]$$

$\frac{A_c m(t)}{2}$  (circled)  
 $\frac{A_c m(t)}{2} \cos 2wt$  (circled)  
filter out

SSB-SC

$$y_1(t) = m(t) \cos wt + \hat{m}(t) \sin wt$$

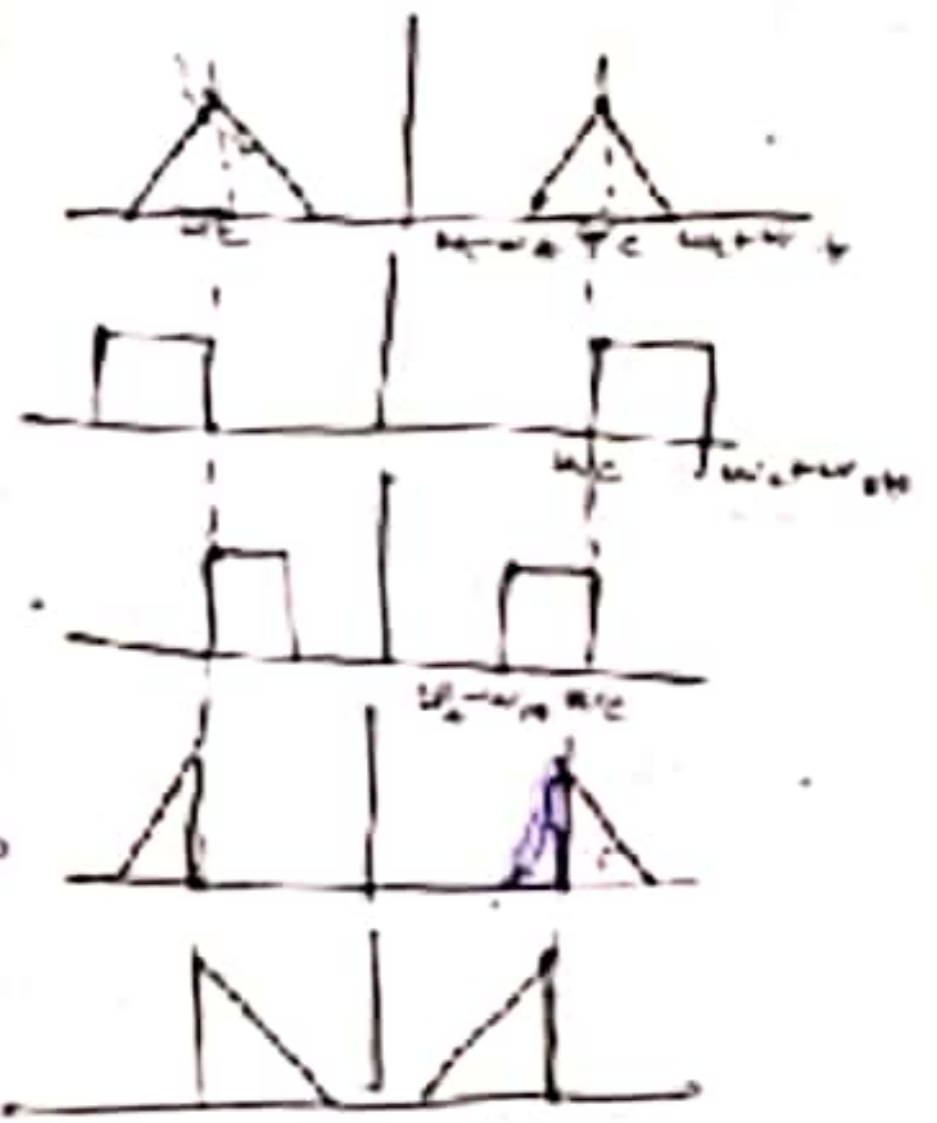
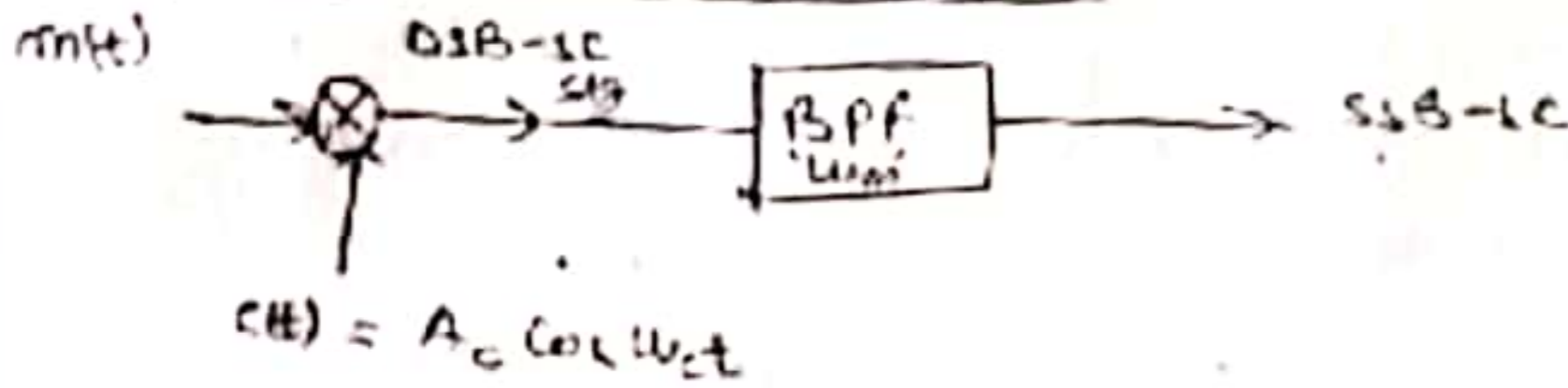
$$y_2(t) = m(t) \cos wt - \hat{m}(t) \sin wt$$

$$= m(t) \left( \frac{1 + \cos 2wt}{2} \right) - \hat{m}(t) \left( \frac{\sin 2wt}{2} \right)$$

$\frac{m(t)}{2}$  (circled)  
 $\frac{m(t)}{2} \cos 2wt + \frac{\hat{m}(t)}{2} \sin 2wt$  (circled)  
filter out

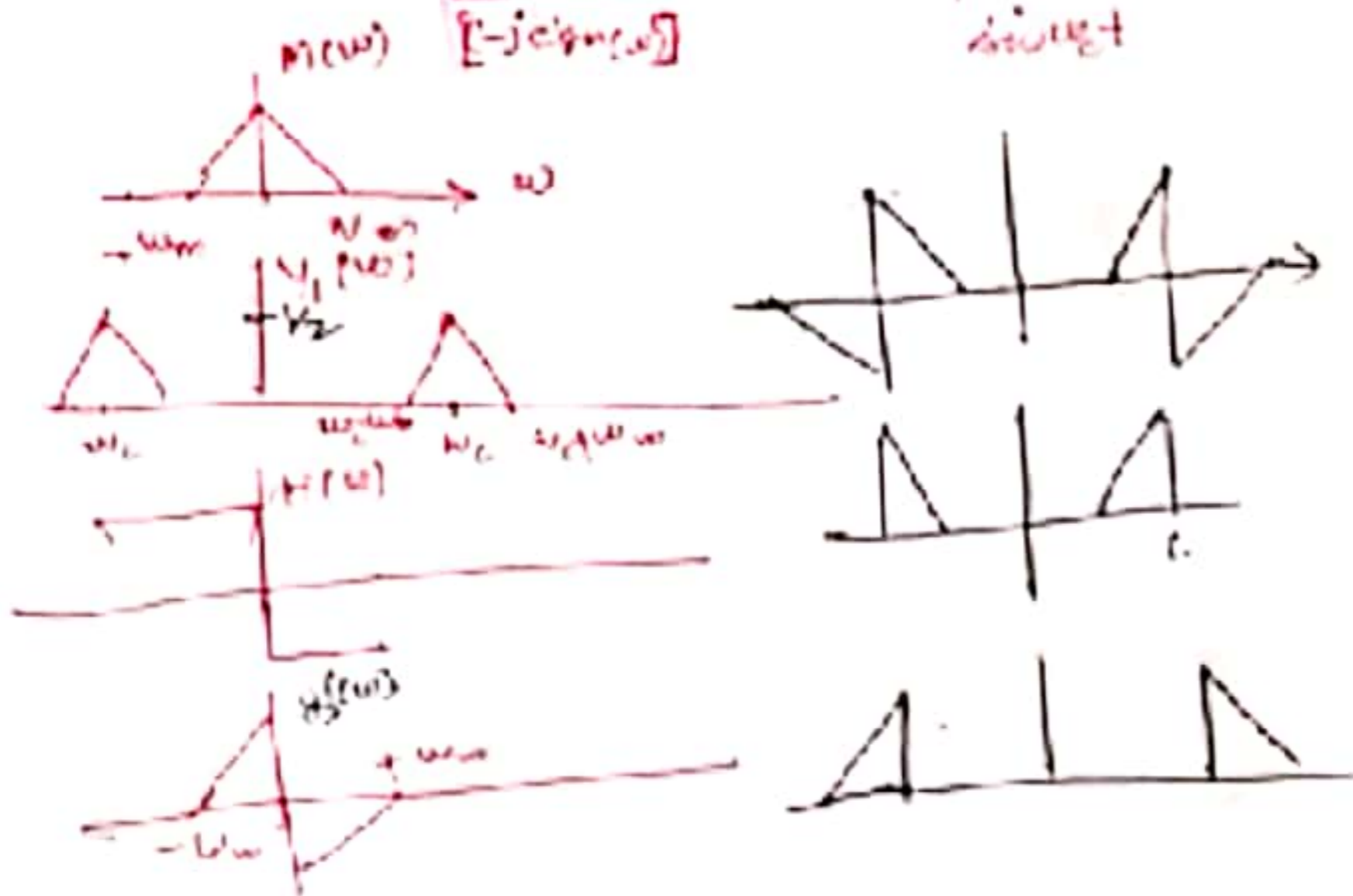
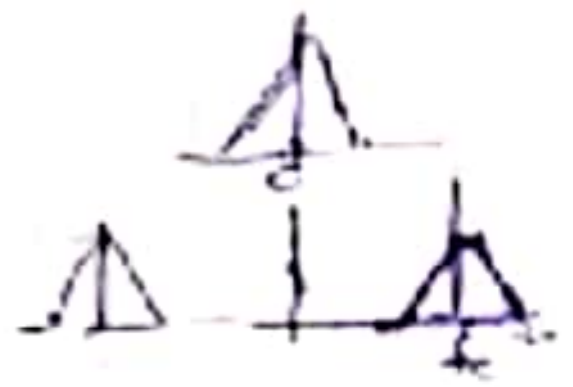
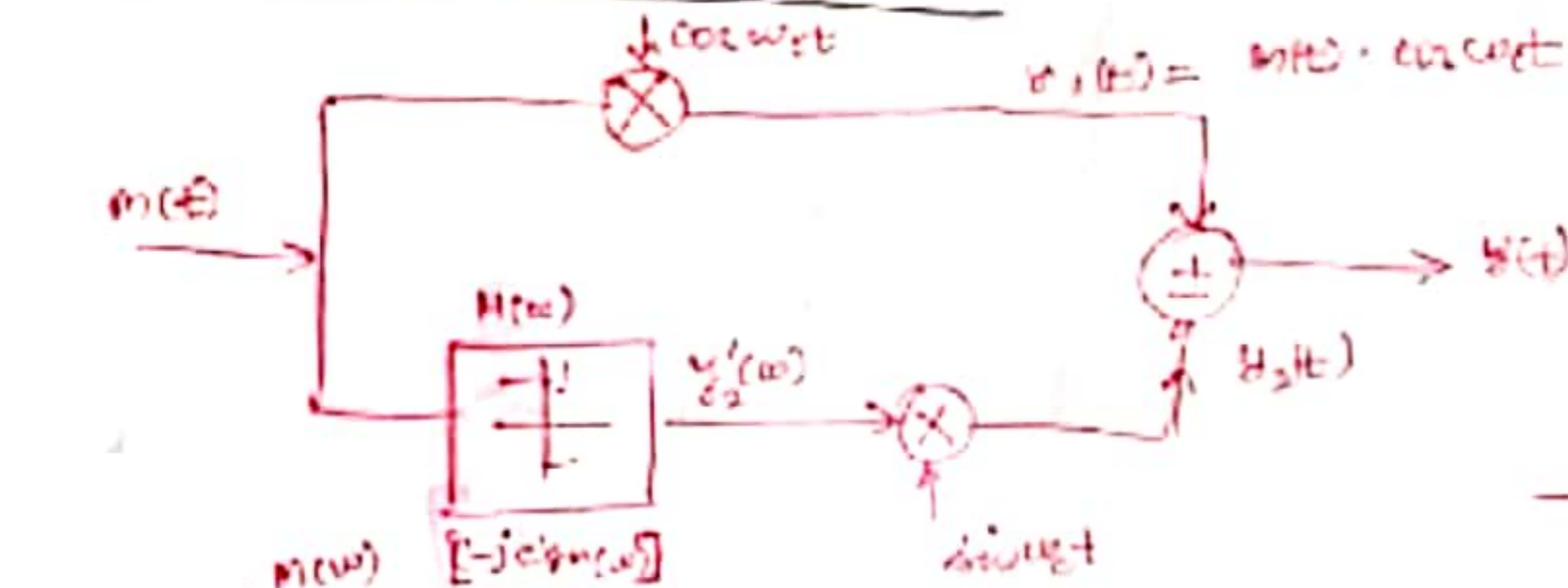
Generation of SSB-SC  $\rightarrow$  Frequency discrimination method  
 $\rightarrow$  Phase discrimination method

Frequency discrimination method



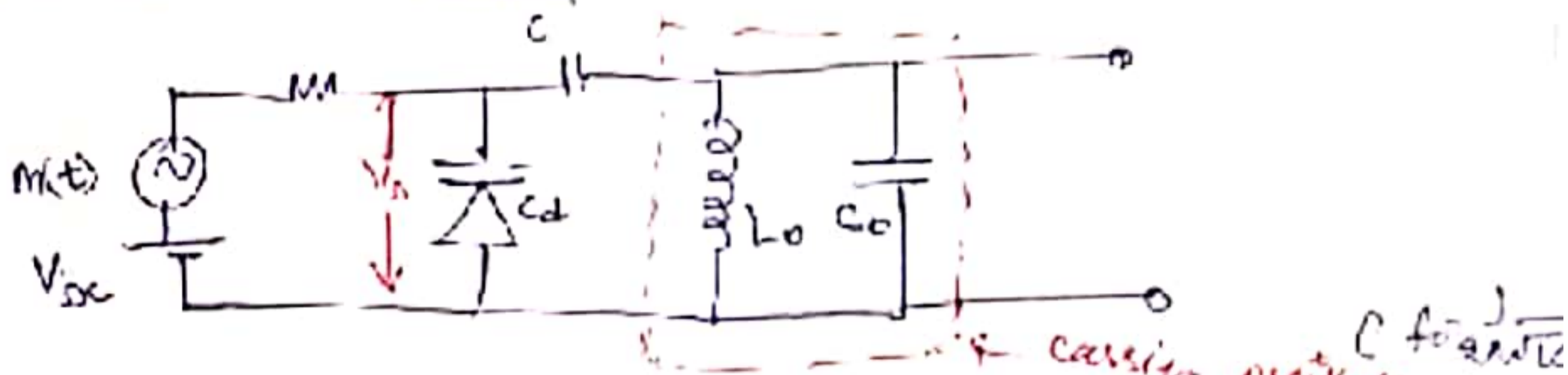
\* In case of frequency discrimination method the band pass filter should be as ideal as possible i.e. transition band should be zero. For this B. of the tuned ckt must be very high which is not practically possible so some part of other sideband is also transmitted. That's why this type of SSB generation is not used.

Phase discrimination method



## Varactor Diode Modulators

→ A varactor diode is a semiconductor diode whose junction capacitance varies linearly with the applied bias. It must operate in reverse biased.



→ The varactor diode is connected in shunt with the tuned circuit of the carrier osc<sup>r</sup>.

The capacitance  $C_d$  of varactor diode.

$$C_d = \frac{K}{V_D} = K (V_D)^{-1/2}$$

where  $V_D = V_{DC} + m(t)$

→ The total capacitance of the osc<sup>r</sup> tank circuit will be  $C_0 + C_d$  and thus the instantaneous freq of oscillation  $f_i$  is

$$f_i = \frac{1}{2\pi \sqrt{L_0 (C_0 + C_d)}}$$

$$f_i = \frac{1}{2\pi \sqrt{L_0 (C_0 + K V_D^{-1/2})}}$$

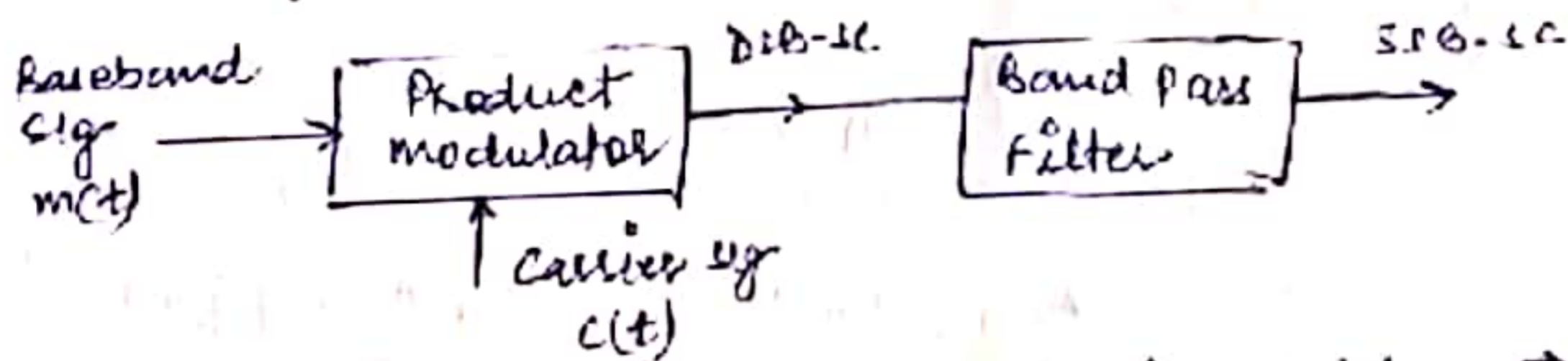
→ The instantaneous freq  $f_i$  of FM signal depends upon  $V_D$  which in turn depends upon the value of modulating signal  $m(t)$ . Thus  $f_i$  also depends upon  $m(t)$  and FM is generated.

### Disadv

In direct method of FM generation, it is not easy to get a high order stability in carrier freq.

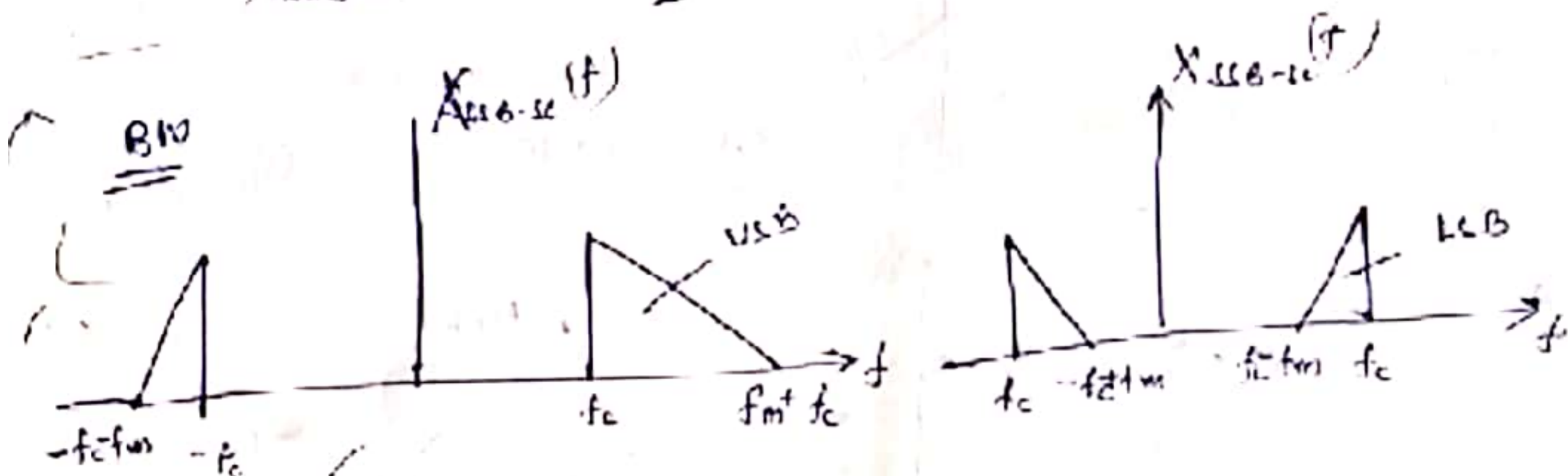
## Single Sideband (SSB-SC)

- Single sideband suppressed carrier modulation is the process in which only upper side-band or lower sideband is transmitted.
- Since both the side band contains same info so instead sending both we can suppress one sideband.



$$X_{SSB-SC}(t) = \frac{A_c A_m}{2} \cos 2\pi (f_c + f_m)t \Rightarrow \text{For USB}$$

$$X_{SSB-SC}(t) = \frac{A_c A_m}{2} \cos 2\pi (f_c - f_m)t \Rightarrow \text{For LSB}$$



so  $B_T = (f_c + f_m) - f_c$

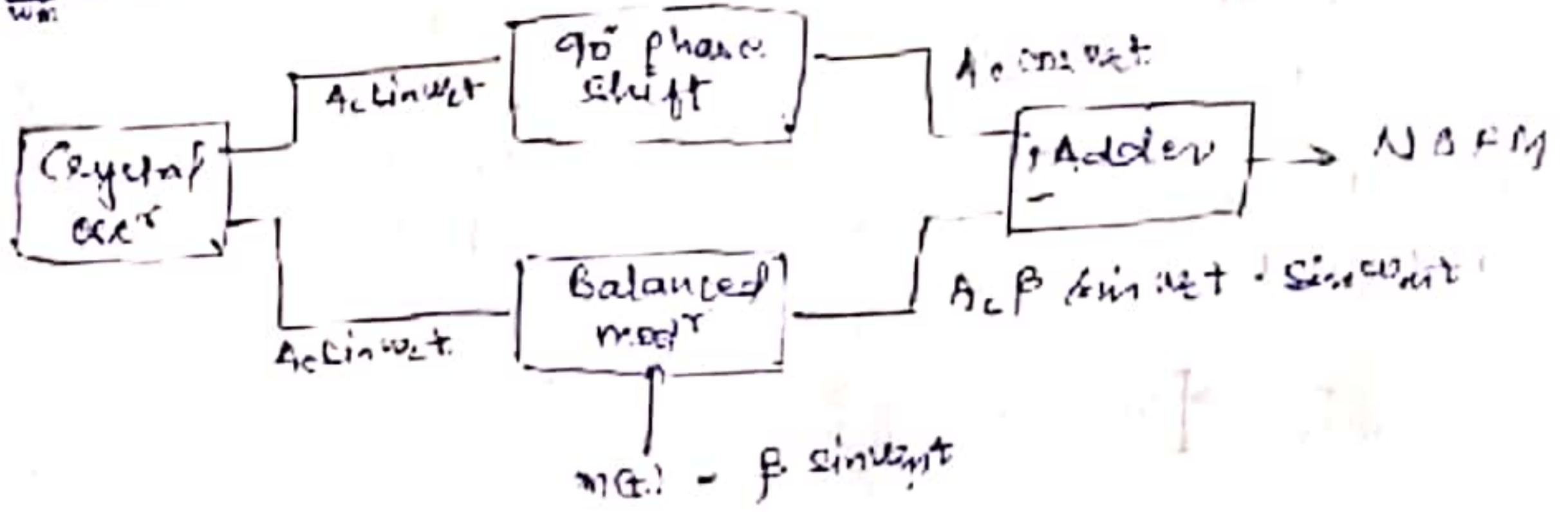
$$\boxed{BW = f_m}$$

### Drawback of SSB

It's filter is very difficult to design (Accuracy is difficult to achieve and costly also).

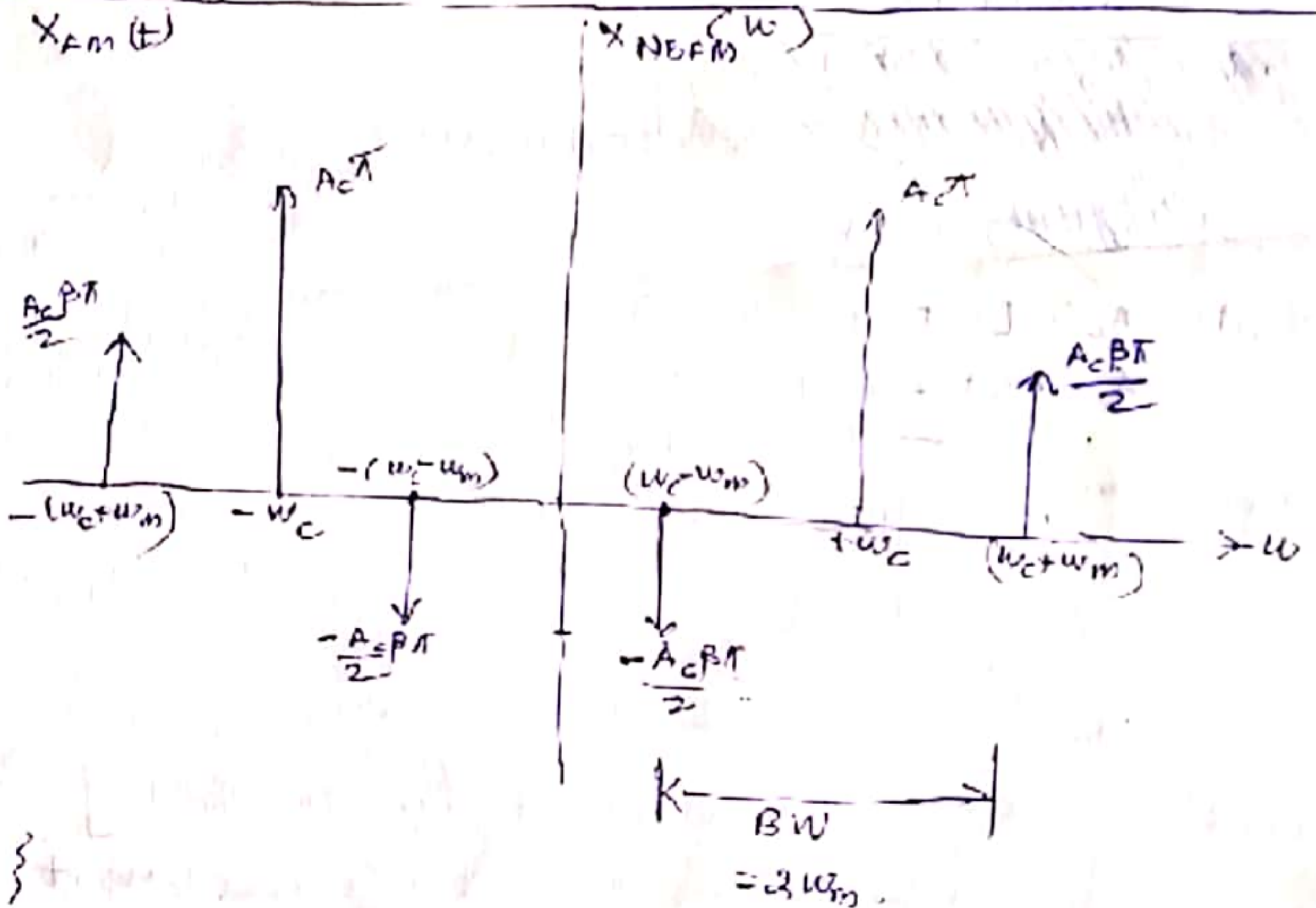
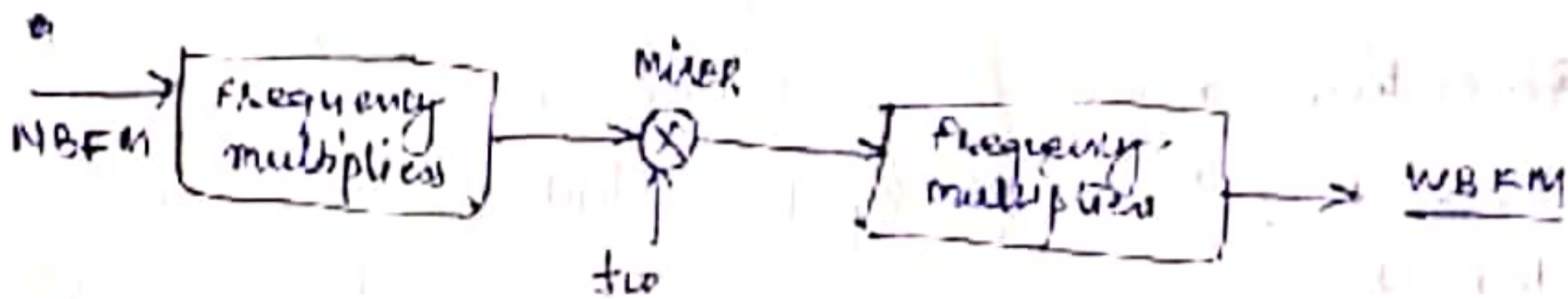
$$m(t) = A_m \cos \omega_m t$$

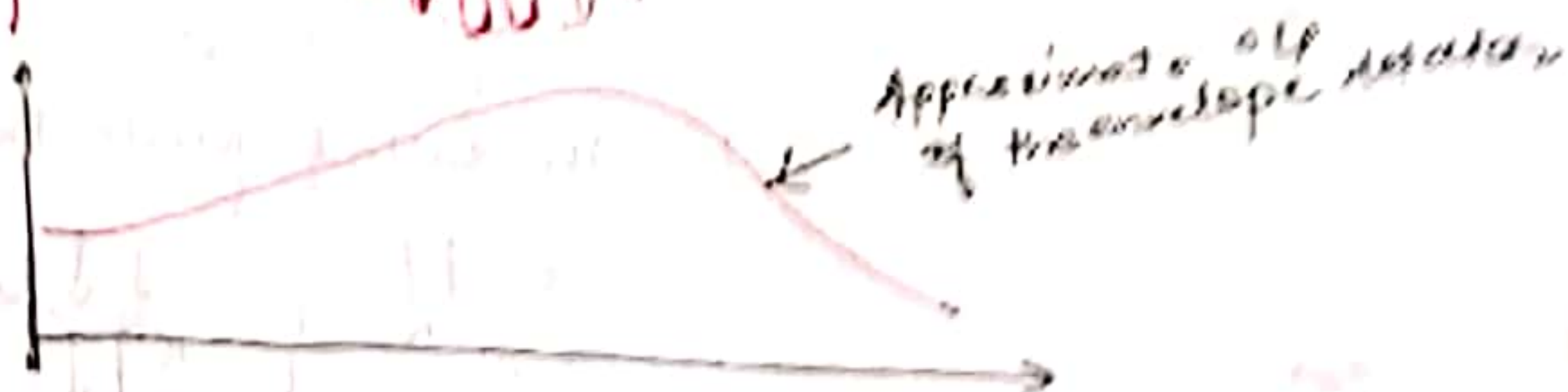
$$= \frac{A_m}{\omega_m} \sin \omega_m t$$



$$y(t) = A_c \cos \omega_c t + A_c \beta \sin \omega_c t \sin \omega_m t$$

This expression represents a narrow band FM





selection of time constant

→ The capacitor C charges through D and R<sub>2</sub> when the diode is ON and it discharges through R<sub>1</sub> when D is off.  
 → The charging time constant  $\tau_c = R_2 C$  must be short as compared to the carrier time period i.e.  $R_2 \ll \frac{1}{f_c}$  so that cap charges rapidly and always follows the applied voltage when the diode is conducting.

→ The discharging time constant  $\tau_d = R_1 C$  must be large i.e.  $\tau_d \gg \frac{1}{f_c}$  so that the cap discharges slowly through the resistor between positive peaks of the carrier wave. However, it should not be so long that the cap voltage does not discharge at the rate of change of the modulating wave, i.e.

$\frac{1}{f_c} \ll R_1 C \ll \frac{1}{\omega}$  → very messy.

① if  $R_1 C \ll \frac{1}{f_c}$



② if  $\frac{1}{f_c} \ll R_1 C$



③  $R_1 C \approx \frac{1}{\omega}$

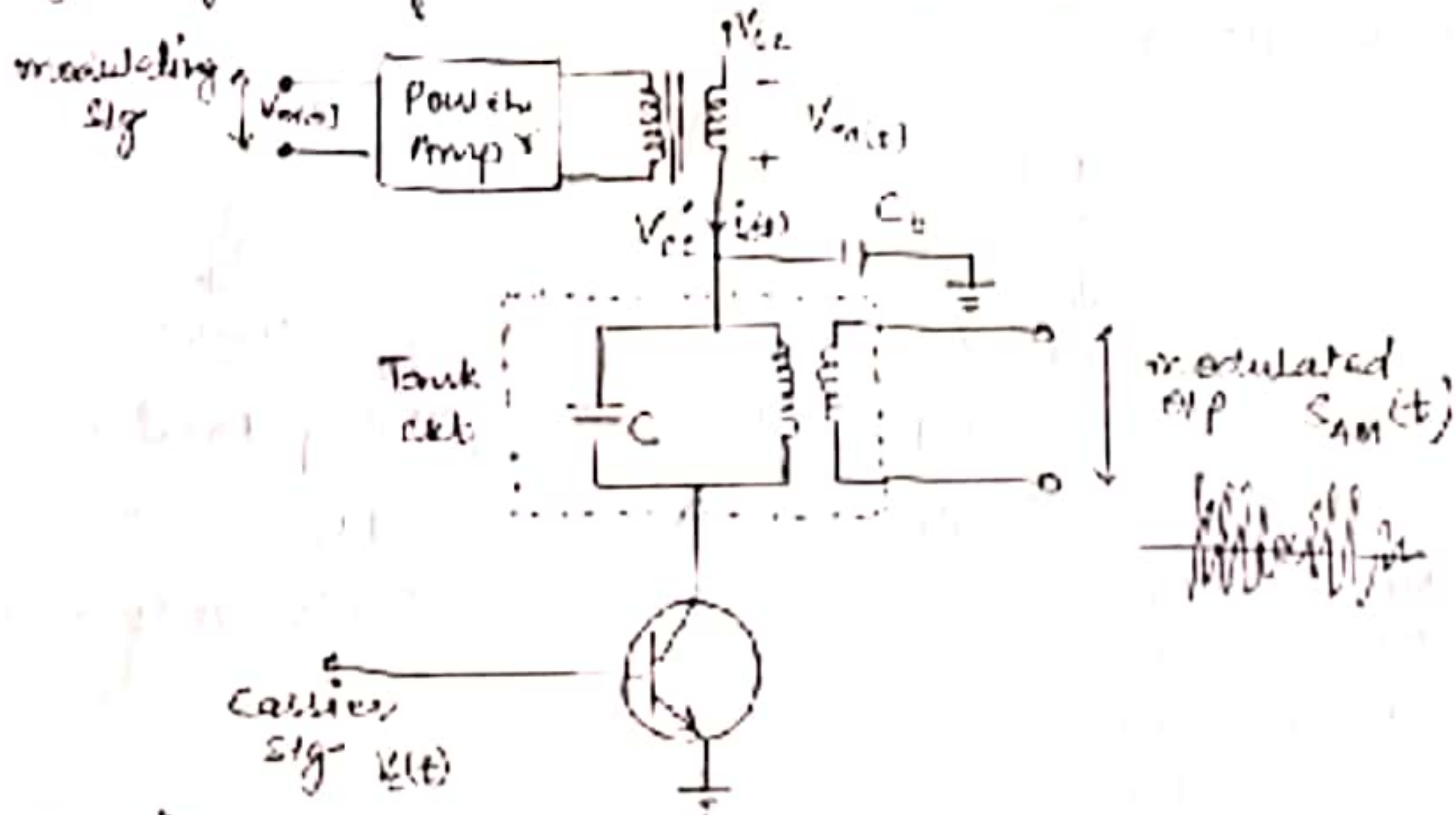


if  $R_1 C \approx \frac{1}{\omega}$  then discharging will be horizontal and the modified output voltage will have many peaks because of that signal clipping occurs.



## Collector Modulator

→ It is a linear type of modulator. In this modulation, linear region of  $ch^2$  of  $T^r$  or Diode is used.



## Construction

- carrier sig is applied at base and modulating sig is applied at collector terminal at AF transformer.
- The modulating sig is amplified through power amp then applied to primary of AF TF.
- Tank ckt is connected at collector as a load from which modulated sig is received.
- Bypass cap<sup>r</sup> is used for protection of AF TF from high freq signal.

## Working

- In this method, the modulating voltage is amplified first then applied to collector for modulation that is why it is known as high level modulation.
  - bias voltage  $V_{cc}$  is superimposed on modulating sig so  $V_{cc}$  bias voltage changes acc. to modulating sig  $m(t)$
- $$V_{cc}' = V_{cc} + m(t)$$



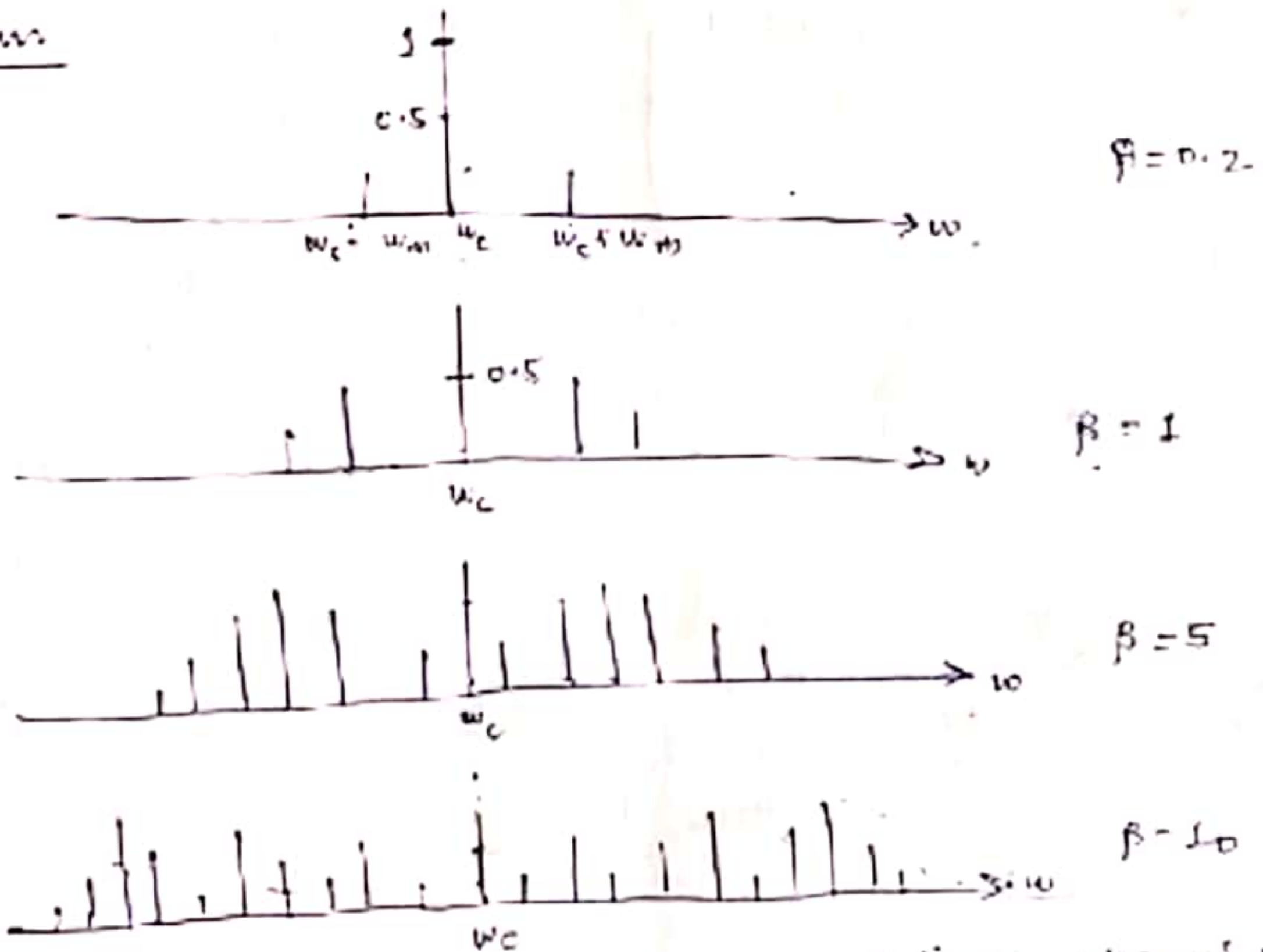
$$S_o(t) = A_c \cos[\omega_c t + \beta \sin \omega_m t]$$

$$S_o(t) = A_c \sum_{n=-\infty}^{\infty} J_n(\beta) \cos(\omega_c + n\omega_m)t$$

→  $J_n(\beta)$  is the Bessel fn of first kind of order  $n$  and argument  $\beta$ .

This expression is not simple due to sine of sine fn. The only way to solve this eq<sup>n</sup> is by Bessel fn.

Spectrum

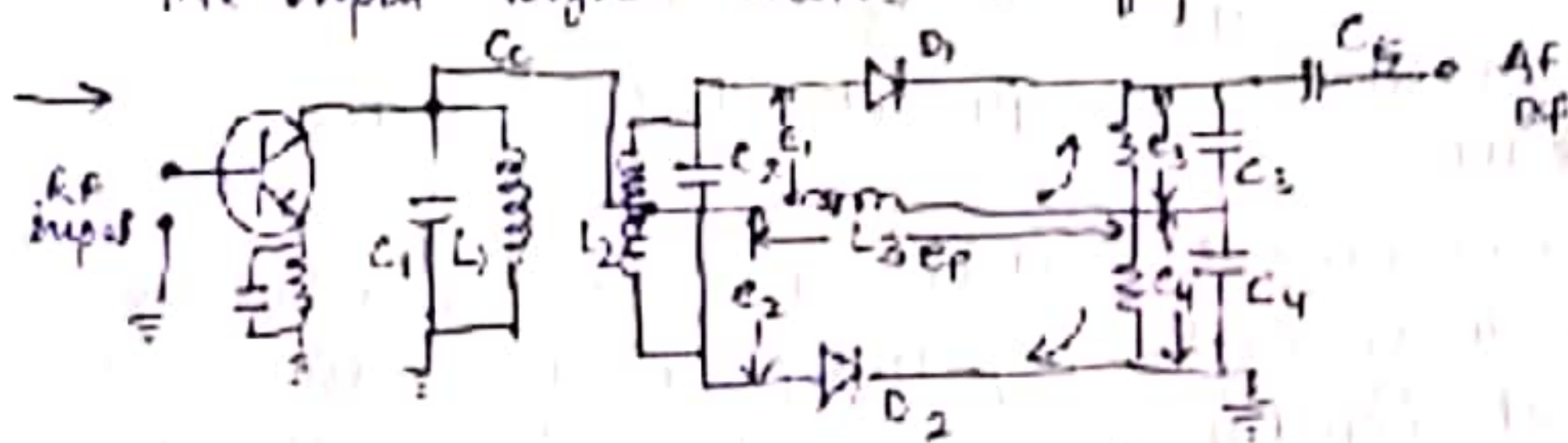


→ The relative amplitudes of the spectral lines depend on the values of  $J_n(\beta)$  and value of  $J_n(\beta)$  becomes very small for large value of  $n$ .

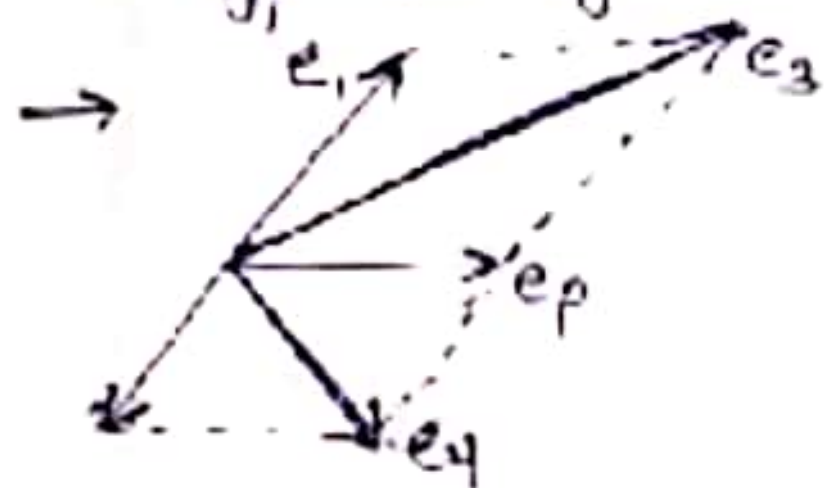
⇒ FM → Narrowband FM {  $\beta$  is small compared to 1 }  
 → wide band FM { large values of  $\beta$  }

## FOSTER SLOTT DISCRIMINATOR

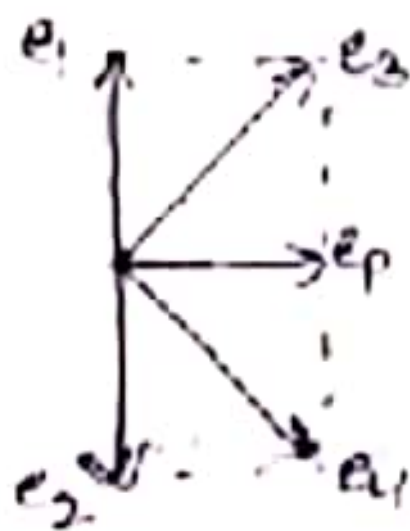
- > The Foster slot discriminator is also known as the phase shift discriminator. It uses a double-tuned or T/F to convert fm variations in the received fm signal to amplitude variations. These amplitude variations are then rectified and filtered to provide a dc output voltage. This voltage varies in both amplitude and polarity as the input signal varies in fm.



- > The collector tank circuit consists of  $C_1$ ,  $L_1$ ,  $C_2$  &  $L_2$  forms the secondary tank circuit. Both tank circuits are tuned to the center fm of incoming fm signal.
- >  $L_3$  is the dc return path for  $D_1$  &  $D_2$ .  $R_L$  &  $R_D$  are load and bypassed by  $C_3$  &  $C_4$  to remove rf.  $C_c$  is coupling cap.



(A) ep in phase resonance



(B) ep in phase at resonance



(C) ep below resonance

### Deep cut resonance

The input signal applied to the primary tank circuit as  $e_p$ . Since coupling capacitor  $C_c$  has negligible reactance at its fm, it choke  $L_2$  is effectively in parallel with primary tank circuit. Also, because  $L_3$  is effectively in parallel with primary tank circuit, input voltage  $e_p$  also appears across  $L_3$ . With voltage  $e_p$  applied to the primary of  $T_1$ , a voltage is induced in the secondary, which causes current to flow in secondary tank circuit. The current flowing in tank circuit causes voltage drops across each half of the secondary. These voltage drops are equal amplitude and opposite phase.

Let  $m(t) = A_m \cos \omega_m t$

→ then in PM

$\phi(t) = k_p m(t) = \frac{k_p A_m \cos \omega_m t}{1}$

↓

Modulation index  $\beta_{PM} = k_p A_m$

→ for FM,  $\phi(t) = k_f \int m(t) dt = k_f \int A_m \cos \omega_m t dt$   
 $= \frac{k_f A_m \sin \omega_m t}{\omega_m}$

↓

Modulation index  $\beta_{FM} = \frac{k_f A_m}{\omega_m}$

So,  $\beta = \begin{cases} k_p A_m & \text{for PM} \\ \frac{k_f A_m}{\omega_m} & \text{for FM} \end{cases} \Rightarrow \text{Modulation index or Max}^m \text{ value of phase deviation}$

Important points about  $\beta$

- In FM  $\beta$  decides the BW of FM.
- $\beta_{FM}$  can be greater than 1
- $\beta$  also decides no. of side bands having significant amplitude

Deviation Ratio

→ The modulation index corresponding to the max deviation and max freq is called as deviation ratio.

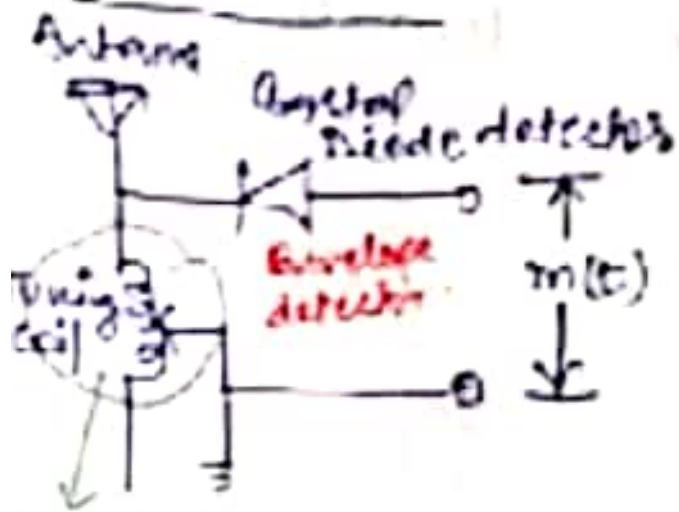
$D = \frac{\text{Max}^m \text{ deviation}}{\text{Max}^m \text{ modulating freq.}} = \frac{\Delta \omega}{\omega_m}$

$D = \frac{\Delta \omega}{\omega_m}$

## Types of Radio Receivers

- ① Crystal radio Rx
- ② Tuned radio freq. Rx
- ③ Super heterodyne radio Rx

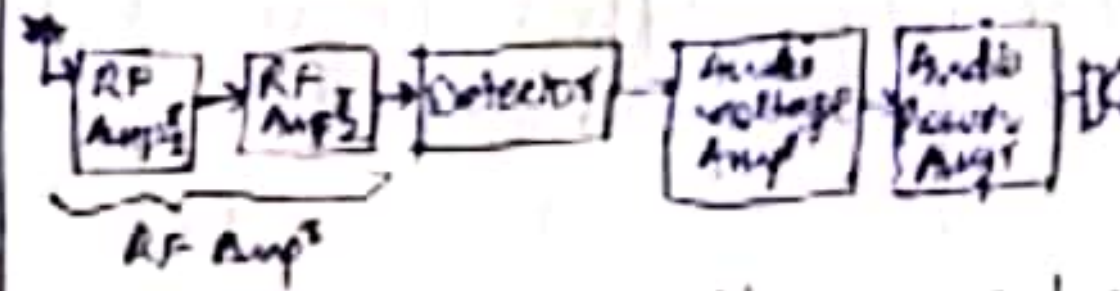
### Crystal Rx



Defined freq. can be selected by changing turns of coil

- Selectivity & sensitivity is very poor
- Amp is not used so weak demodulated signal

### TRF Rx

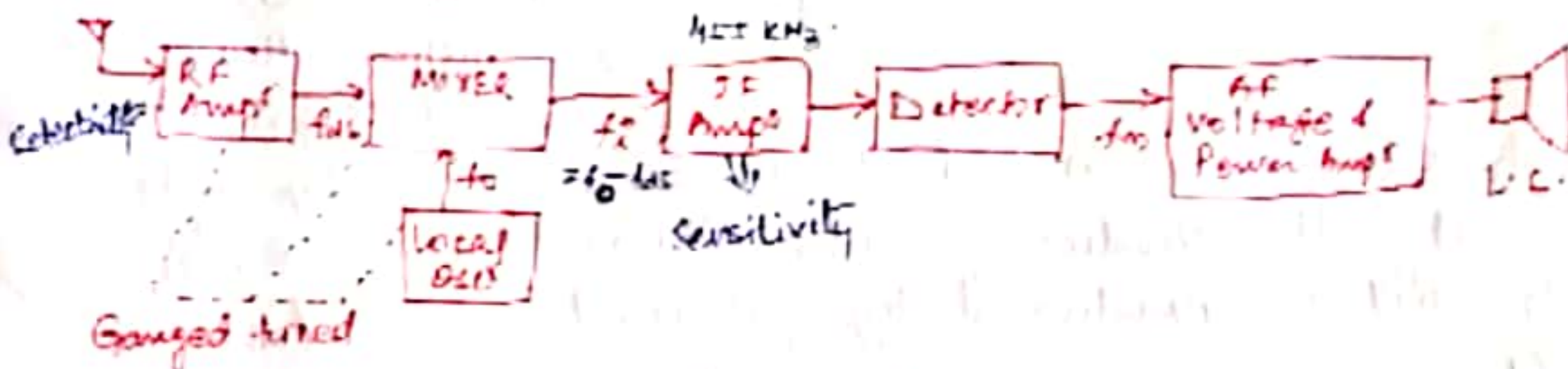


- Good only for medium wave freq but poor performance at higher freq.
- Intractable due to multiple RF amps, variation in B.W. Poor selectivity
- Simple circuit & good sensitivity

### SHRR

A superheterodyne Rx, often shortened to Superhet, is a type of Radio Rx that uses freq. mixing to convert a received signal to a fixed intermediate freq. which can be more conveniently processed than the original carrier freq.

## Super Heterodyne radio Receiver



$$f_0 = f_{c} + f_i$$

$$f_i = f_0 - f_{c} \rightarrow \text{is selected}$$

### Working

- The received signal is amplified by rf amp which is a tuned Amp. Amplified signal is passed on to a mixer. here of carrier is mixed with  $f_0$  generated by local osc. The process of mixing is called heterodyning.  $f_0$  is selected to be above  $f_{c}$ .
- Mixer generates sum and difference of freq ( $f_0 + f_{c}$ ) and ( $f_0 - f_{c}$ ). ( $f_0 + f_{c}$ ) eliminated by a filter. The difference freq ( $f_0 - f_{c}$ ) is called intermediate freq carrier.

## Tuned Radio freq Rx

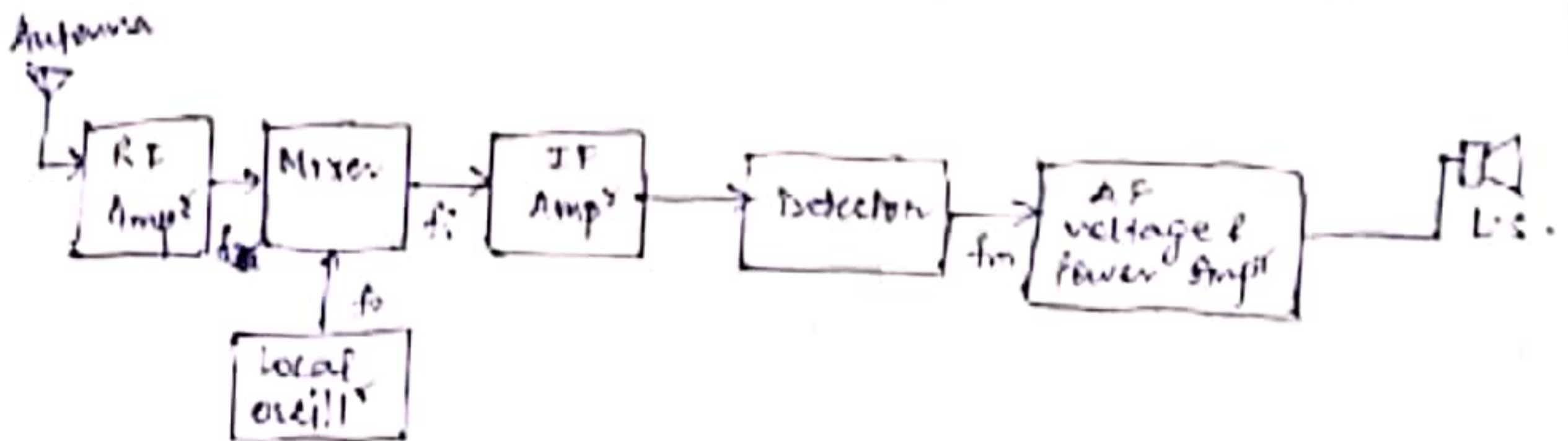


→ works well on medium waves, but performs poor on high radio freq.

## Super heterodyne Receiver

The process of mixing two sig having diff freq to produce a new freq.

→ Superheterodyne is based on principle of heterodyning.



- Mixer generates sum and difference of freq i.e. the mixer output consists of  $f_c + f_r$  and  $f_c - f_r$ .  
 $f_c + f_r$  is eliminated by filter  
 $f_c - f_r$  is called intermediate freq "fi"

• Super heterodyne Rx suffers from major drawback known as image freq problem

• If a freq  $f_{ci}$  manages to reach the mixer

$$f_{ci} = f_{osc} + f_i \quad (f_{osc} = f_c + f_i)$$

$$= f_c + f_i + f_i$$

$$f_{ci} = f_c + 2f_i$$

The rejection of an image freq by a single tuned circuit may be defined as the ratio of the gain at sig freq to the gain at image freq

$$\alpha = \sqrt{1 + Q^2 p^2} \quad \text{where } p = \frac{f_{ci} - f_c}{f_c} = \frac{f_i}{f_c}$$

$Q \rightarrow$  quality factor

## Transmission BW of FM :

→ Theoretically, an FM wave contains an infinite no of side frequencies and consequently BW required is also infinite. Most of the power of FM wave resides in a finite no of sidebands.

→ Carson generalized the BW formula for an FM wave as

$$B_T = 2(\beta + 1) f_m$$

in Hz

$$B_T = 2(\beta + 1) \omega_m$$

in rad/s

→ For Narrowband FM

$$B_T = 2 f_m$$

$$\left\{ \beta \ll 1 \right\}$$

For wideband FM

$$B_T = 2\beta f_m$$

$$\left\{ \beta \gg 1 \right\}$$

→ In terms of deviation ratio the BW is

we know  $\beta = \frac{\Delta f}{f_m}$  so  $\Delta f = \beta f_m$

$$B_T = 2(\beta + 1) f_m = 2\beta f_m + 2f_m$$
$$= 2\Delta f + 2f_m$$

$$B_T = 2(\Delta f + f_m)$$

Because the winding is inductive, voltage is  $90^\circ$  out of phase with current in it. ~~and~~

→ The voltage applied to the anode of  $D_1$  is the vector sum of voltages  $e_p$  and  $e_1$

$$e_3 = e_p + e_1$$

→ The voltage applied to  $D_2$  is vector sum of  $e_p$  &  $e_2$

$$e_4 = e_p + e_2$$

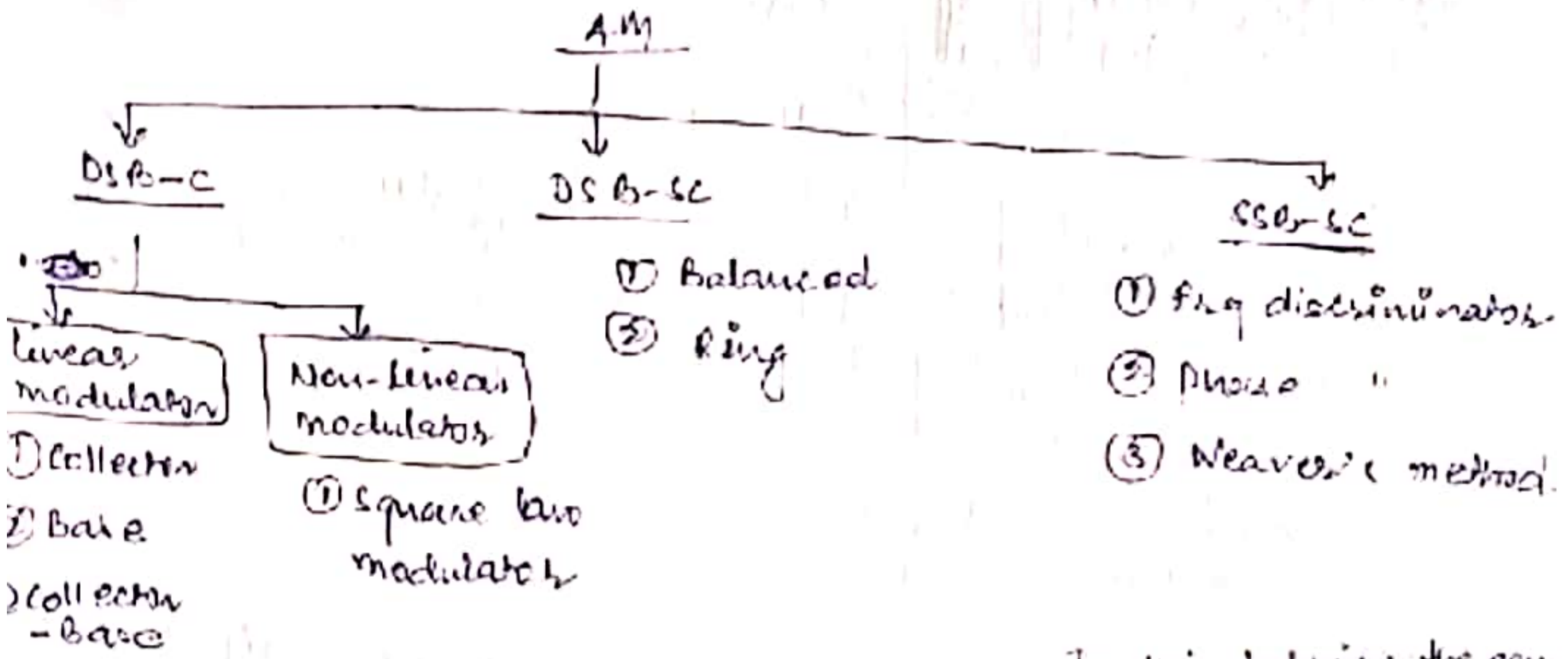
→ At resonance  $e_3 = e_4$

→ The diodes conduct on opposite half cycles of the input waveform

Operation above resonance : A phase shift occurs when an input freq higher than center freq is applied and current & voltage phase relationship changes. When tuned ckt operates at above resonance, the inductive reactance of coil  $\uparrow$  & capacitive reactance of cap  $\downarrow$ . Above resonance the tank ckt acts like an inductor, secondary current lags  $e_p$ ,  $e_1$  &  $e_2$  still out of phase

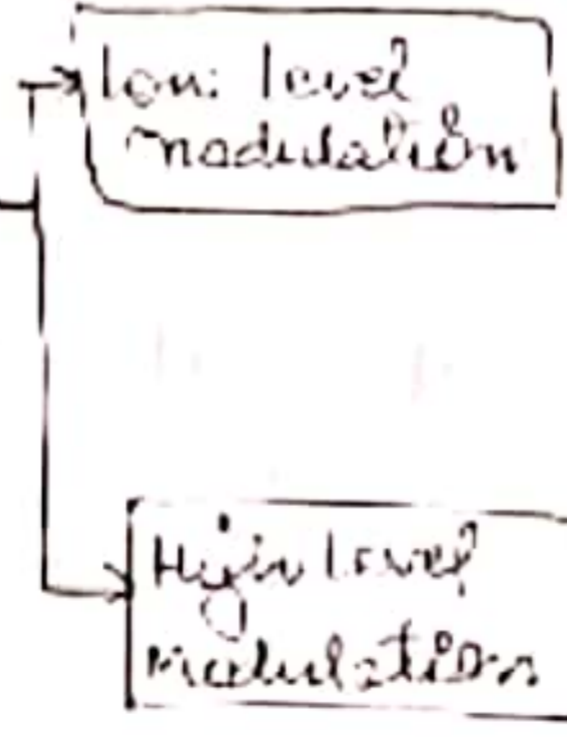
Collector Modulators } DSB-C  
 Base Modulators }

Balanced Modulators → DSB-SC



Collector Modulator

Generation of AM Signal



In this technique the generation of AM wave takes place in initial stage of amplification i.e. at low power level. The generated AM sig is then amplified using no. of amplifier stages.

In high level mod the generation of AM wave takes place in the final stage of amplification & therefore mod circuitry has to handle high power.



## Disadvantages of AM (DSB-C)

- The carrier of AM wave does not convey any information and we know

$$P_T = P_c + \frac{m^2}{4} P_c + \frac{m^2}{4} P_c$$

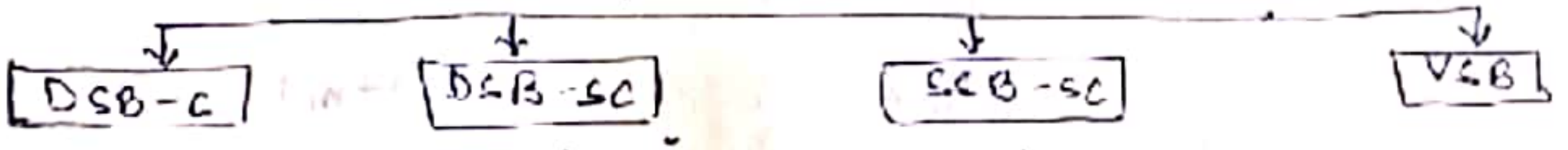
In AM for 100% modulation about 67% of the total power is consumed in transmitting carrier.

→ So power is wastage

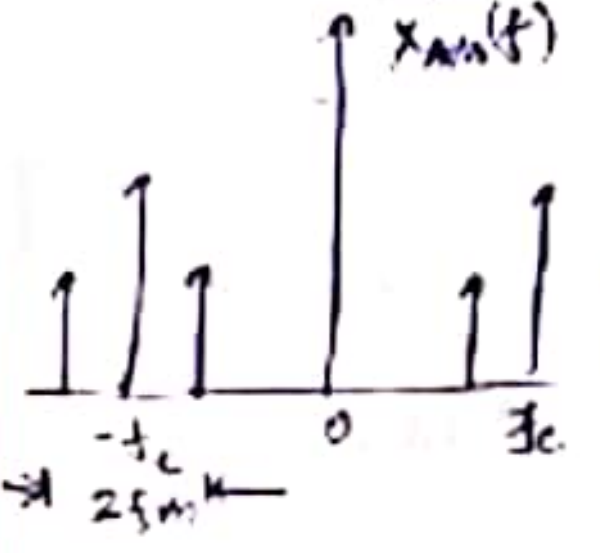
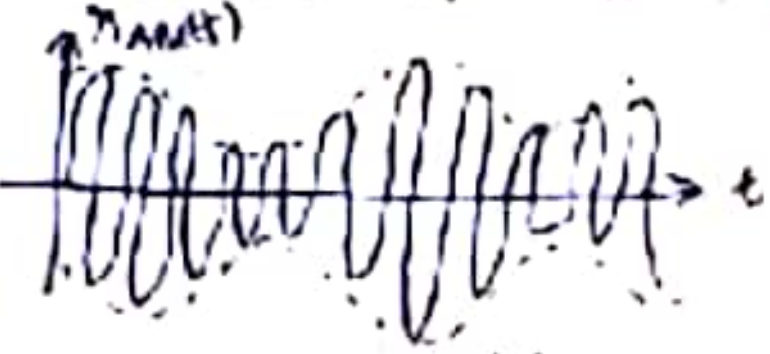
- We know that two side bands are mirror image of each other and all the info can be conveyed by one of the sideband only.

→ Hence DSB-C system is BW inefficient system.

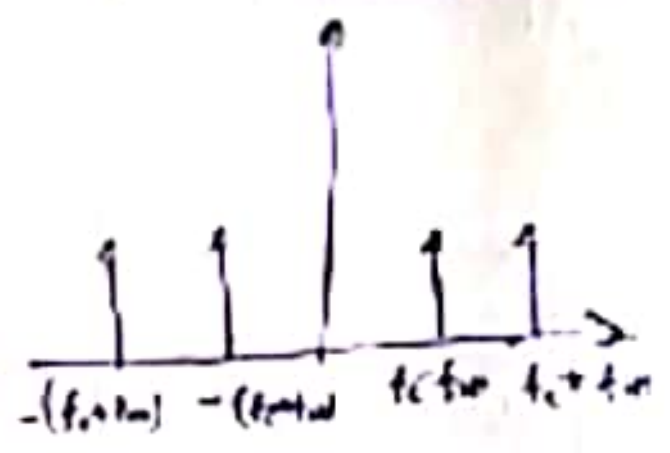
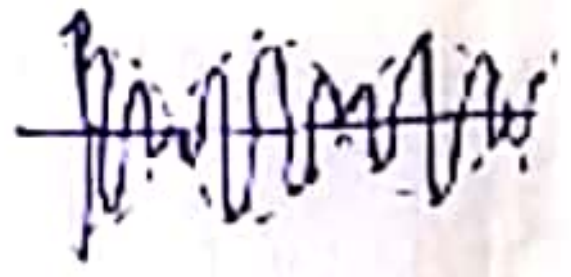
### AM



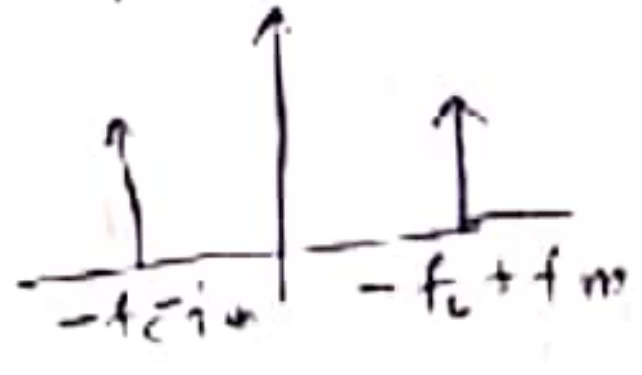
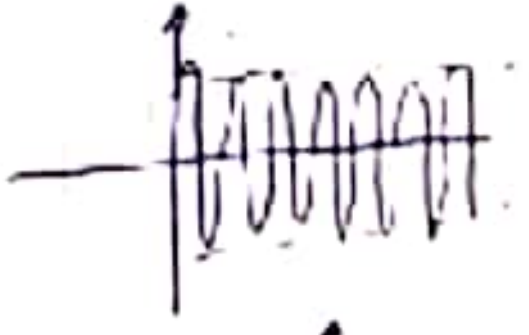
- Standard AM



- Carrier is suppressed

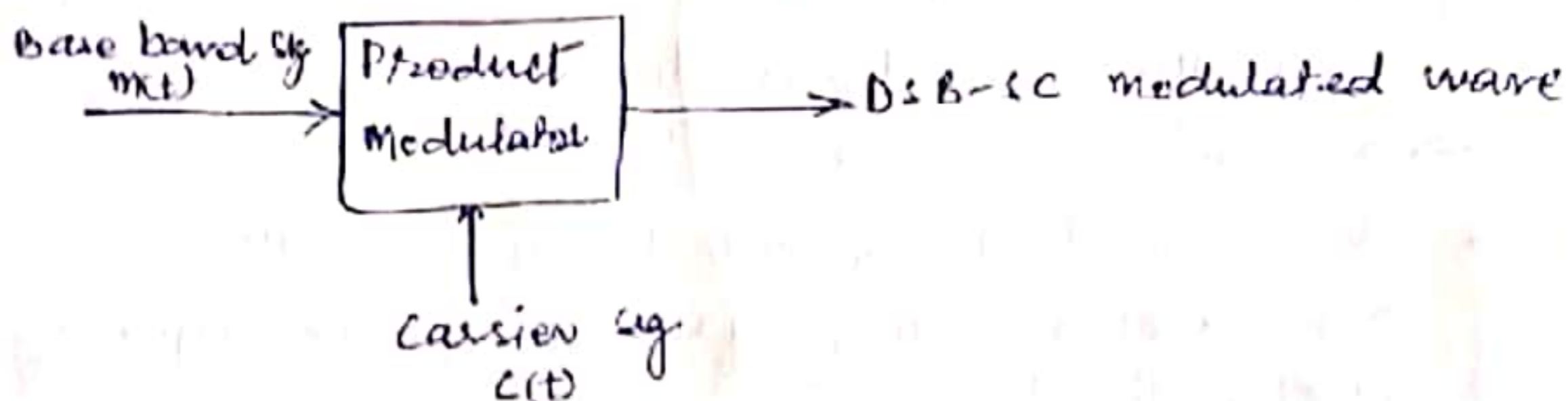


- Carrier + one side band is suppressed



DSB-SC → In this modulation, only upper side band and lower sidebands are transmitted.

→ We can obtain DSB-SC modulation by taking the product of the carrier  $c(t)$  and modulating sig  $m(t)$  which is known as product modulator.



$$\text{if } \begin{cases} c(t) = A_c \cos 2\pi f_c t \\ m(t) = A_m \cos 2\pi f_m t \end{cases}$$

$$\begin{aligned} \text{then, } X_{\text{DSB-SC}}(t) &= c(t) \cdot m(t) \\ &= (A_c \cos 2\pi f_c t) \cdot (A_m \cos 2\pi f_m t) \\ &= A_c A_m \cos 2\pi f_c t \cdot \cos 2\pi f_m t \end{aligned}$$

$$= \frac{A_c A_m}{2} [2 \cos 2\pi f_c t \cdot \cos 2\pi f_m t]$$

$$\because 2 \cos A \cos B = \cos(A+B) + \cos(A-B)$$

$$\text{So, } X_{\text{DSB-SC}}(t) = \frac{A_c A_m}{2} \left\{ \cos 2\pi (f_c + f_m) t + \cos 2\pi (f_c - f_m) t \right\}$$

we can see from this eqn that in DSB-SC there is only upper and lower side bands and carrier is absent.

## frequency domain description of DSB-SC

$$x_{\text{DSB-SC}}(t) = m(t) \cdot c(t) \\ = A_c m(t) \cos 2\pi f_c t$$

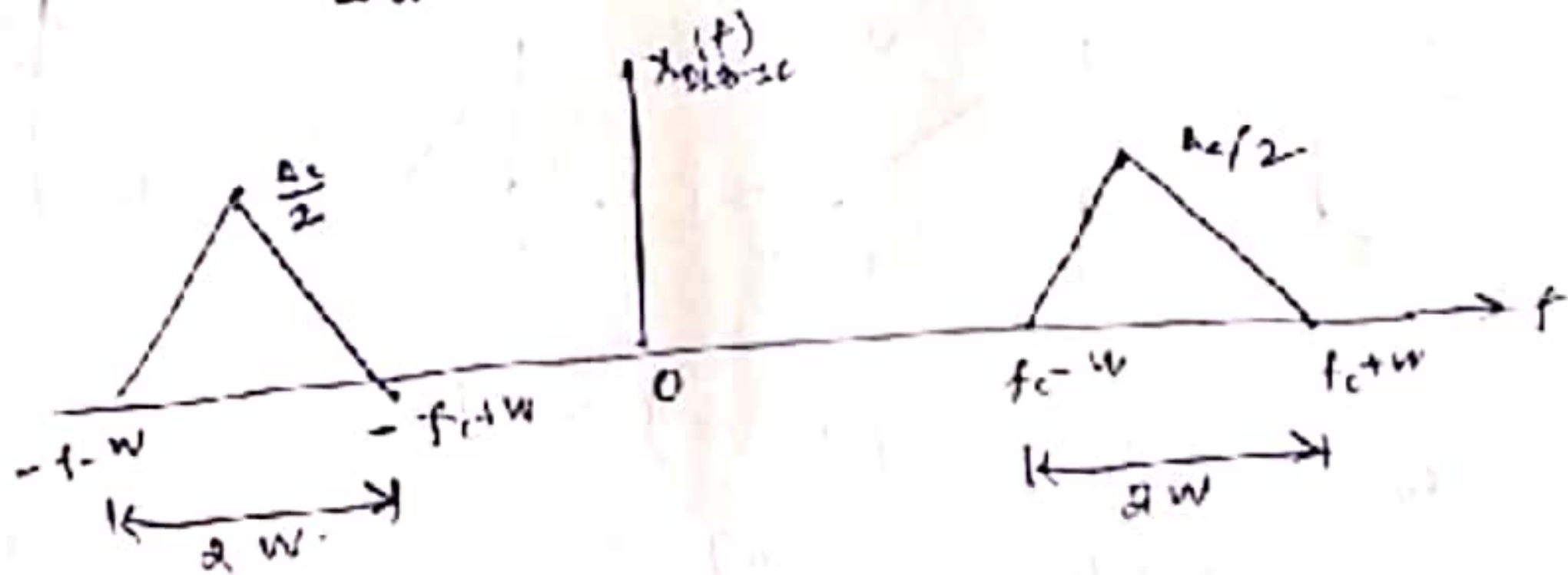
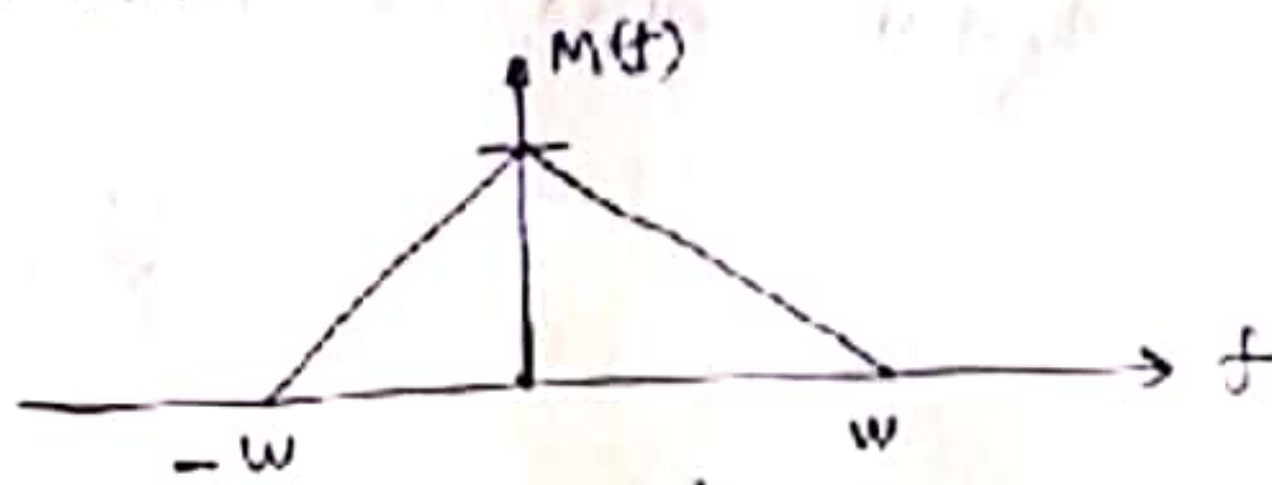
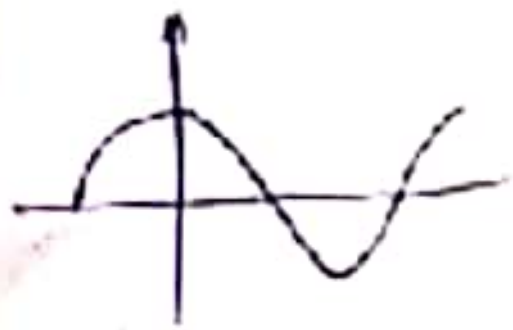
↓ F.T.

$$X_{\text{DSB-SC}}(f) = \text{F.T.} \left\{ A_c m(t) \cos 2\pi f_c t \right\}$$

$$= A_c \left\{ m(t) \left( \frac{e^{j2\pi f_c t} + e^{-j2\pi f_c t}}{2} \right) \right\}$$

$$= \frac{A_c}{2} \text{FT} [m(t) e^{j2\pi f_c t}] + \frac{A_c}{2} \text{FT} [m(t) e^{-j2\pi f_c t}]$$

$$X_{\text{DSB-SC}}(f) = \frac{A_c}{2} M(f - f_c) + \frac{A_c}{2} M(f + f_c)$$



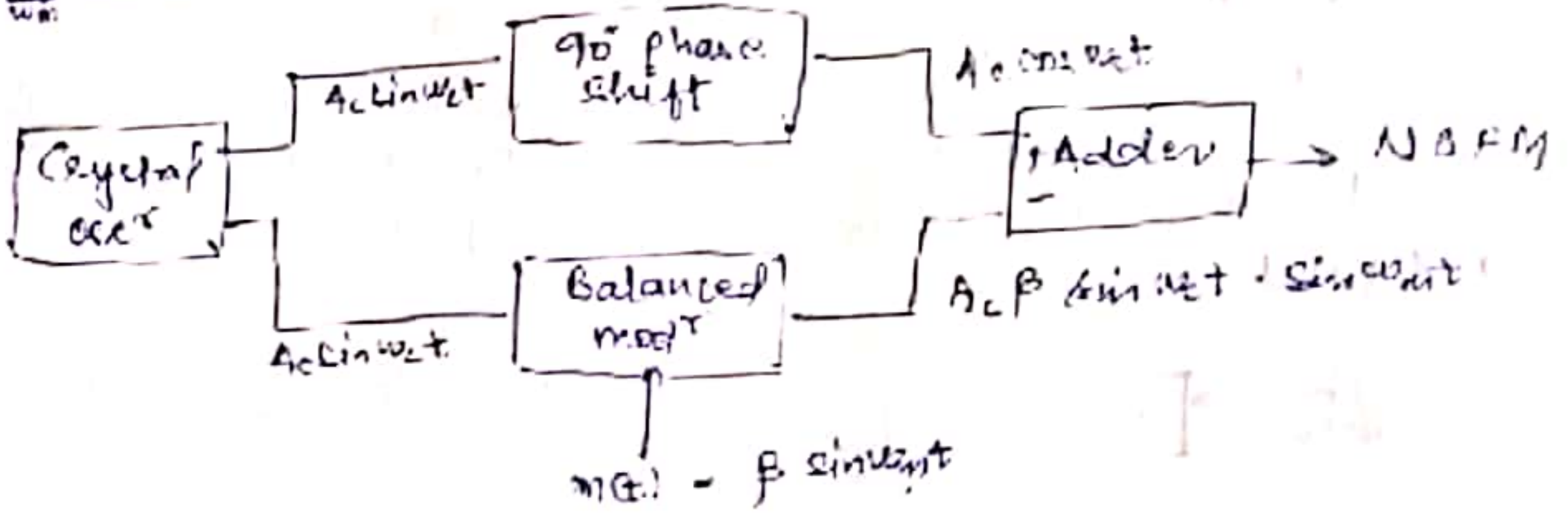
Transmission BW

$$B = (f_c + W) - (f_c - W) = 2W \text{ Hz}$$

→ Thus the transmission BW of DSB-SC is same as that of the standard AM.

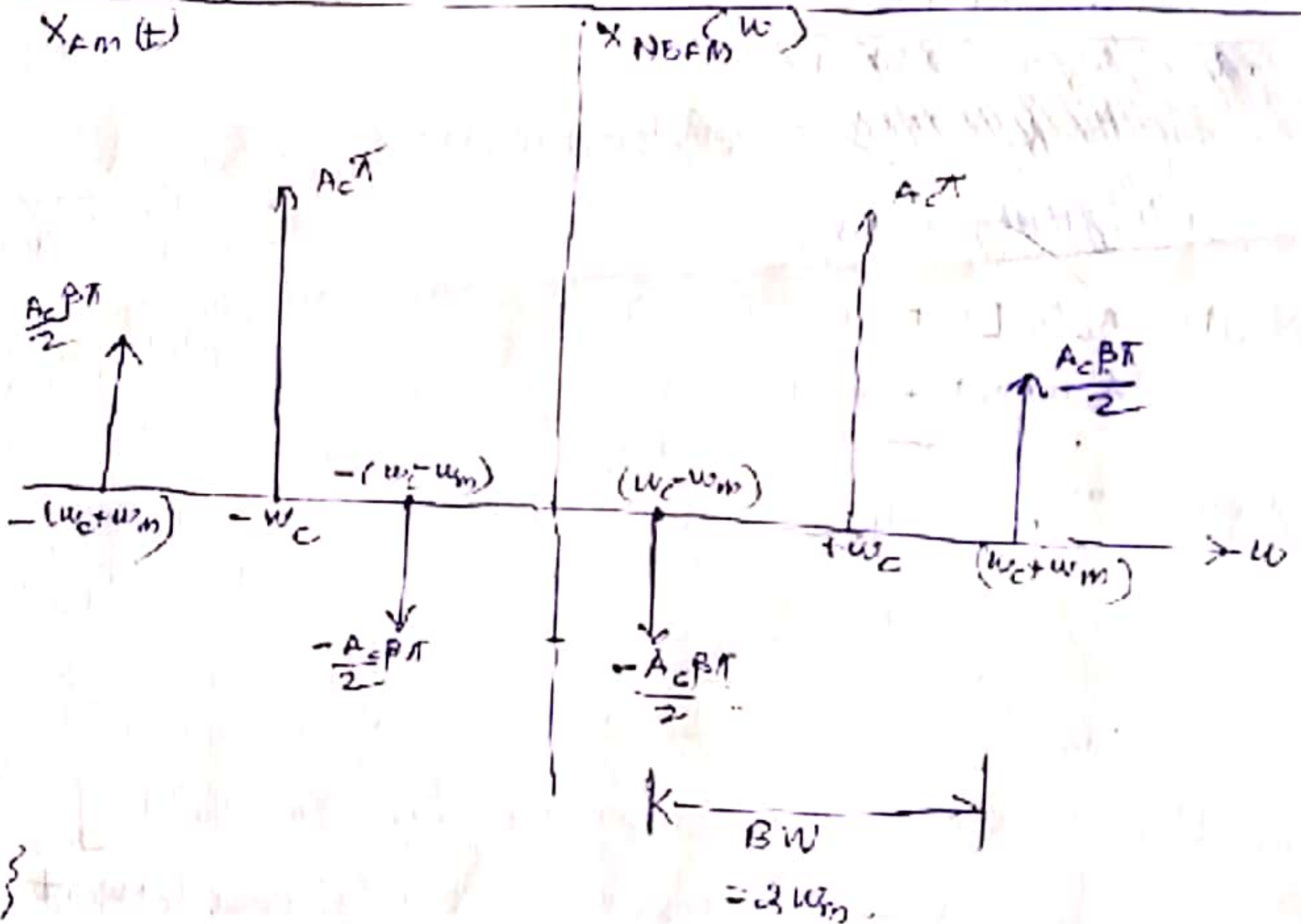
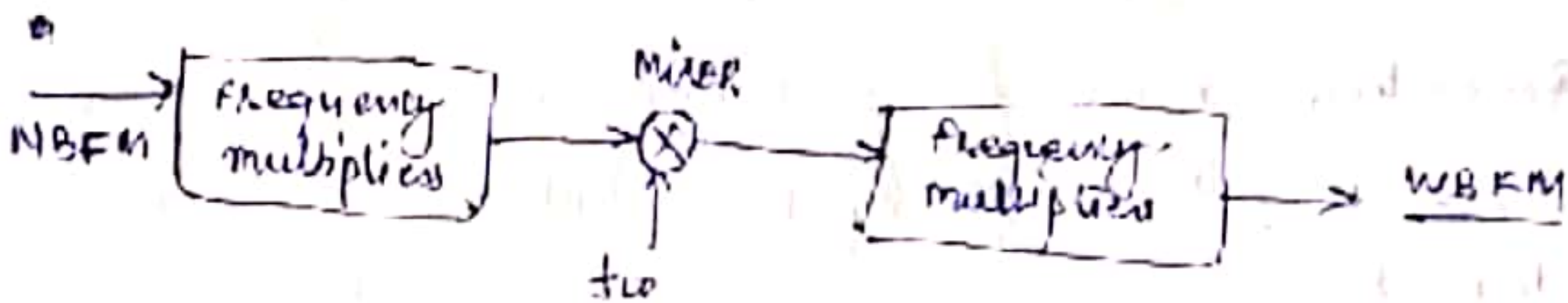
$$m(t) = A_m \cos \omega_m t$$

$$= \frac{A_m}{\omega_m} \sin \omega_m t$$



$$y(t) = A_c \cos \omega_c t + A_c \beta \sin \omega_c t \sin \omega_m t$$

This expression represents a narrow band FM



## Operation

- SSB signal can be generated by receiving two separate simultaneous DSB modulations and combining them suitably depending on the desired sideband.
- The incoming msg sig  $m(t)$  and  $\cos \omega_c t$  of carrier  $\omega_c$  are applied to the balanced modulator 'A'. This balanced modulator produces a DSB-SC wave that translates the freq spectrum of  $m(t)$  symmetrically spaced about the carrier freq  $f_c$ .
- The Hilbert transform of  $m(t)$  i.e.  $\hat{m}(t)$  is applied to second balanced modulator, producing a DSB-SC wave that contains sidebands having identical amplitude spectrum as those of modulator 'A' but of a different relative phase.

$$\text{Adder output} = m(t) A_c \cos \omega_c t \pm \hat{m}(t) \sin \omega_c t$$

In this way both forms of SSB waves can be generated.

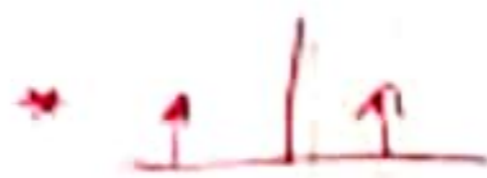
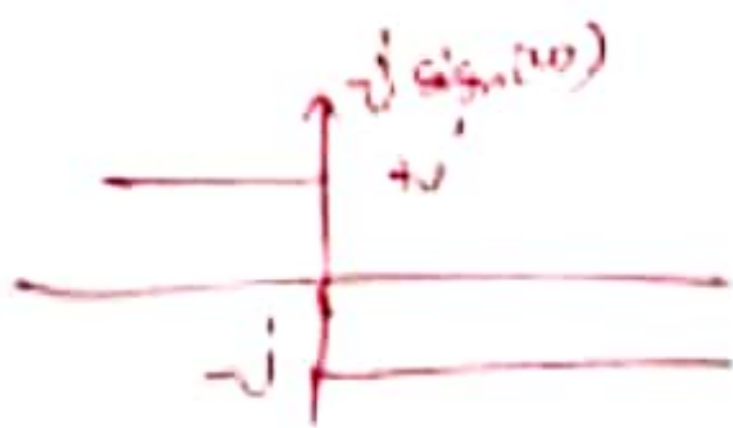
- Hilbert TFA is the method of separating the sig. with respect to their phase contents & not with their freq.
- Hilbert transform separates the sig with a phase diff. of  $90^\circ$  to them.

$x(t) \rightarrow \hat{x}(t)$

$$\hat{x}(t) = x(t) * \frac{1}{\pi t}$$

$$= \int_{-\infty}^{\infty} \frac{x(\tau)}{\pi(t-\tau)} d\tau$$

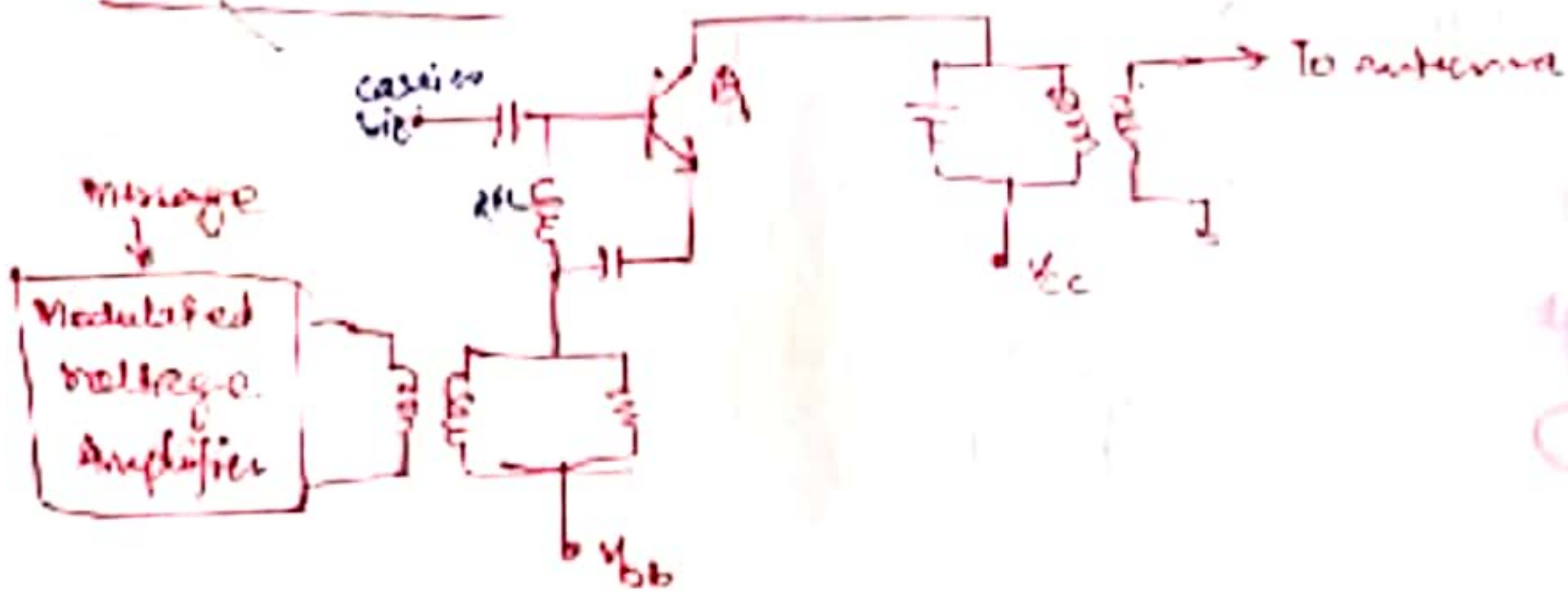
$$\hat{X}(\omega) = X(\omega) \cdot [-j \operatorname{sgn}(\omega)]$$



$\Rightarrow$



## Base Modulator



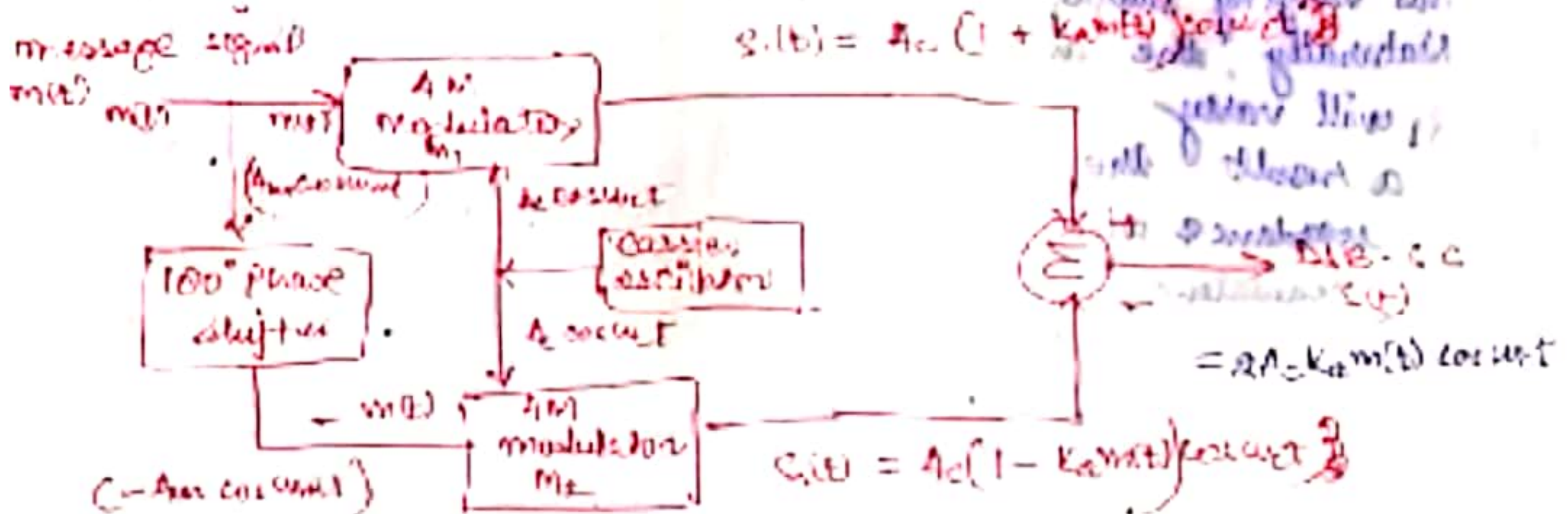
- In this carrier signal is also applied at base.
- AFC is used to isolate high freq signal with audio TF.
- Modulation is done at base. At collector, amplified sp is collected.
- Since amplification process is done so it is a low level modulation.

## Balanced Modulator

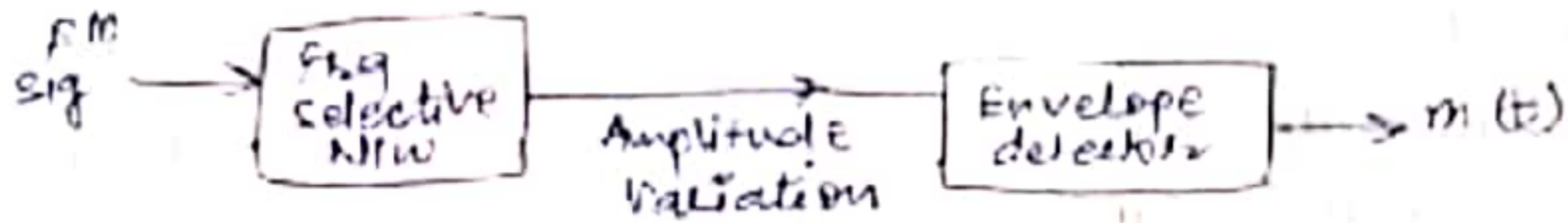
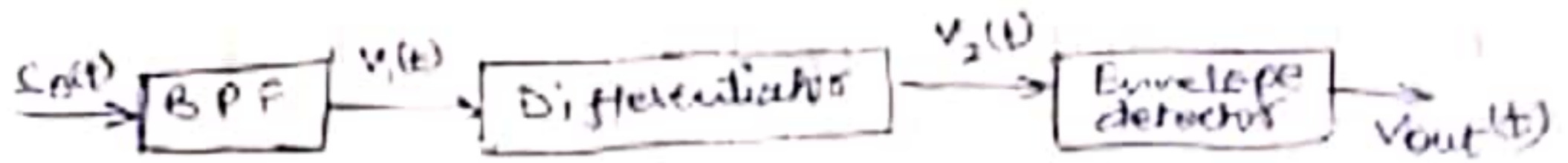
→ A DSB-SC wave is basically the multiplication of the modulating sig  $m(t)$  with carrier wave  $c(t)$ . We need to use a device called product modulator.

① Balanced modulators

② Ring modulators



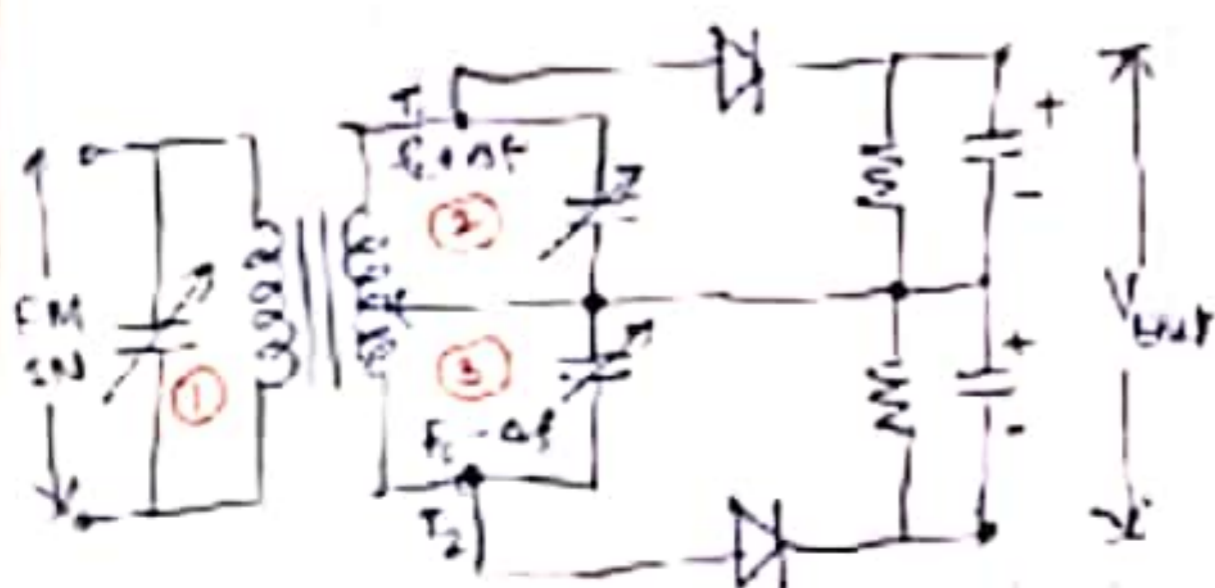
Thus, except for a scaling factor  $2k_a$ , the OP of the balanced modulator is equal to the product of the modulating sig  $m(t)$  and the carrier wave  $c(t)$ . It is the DSB-SC signal.



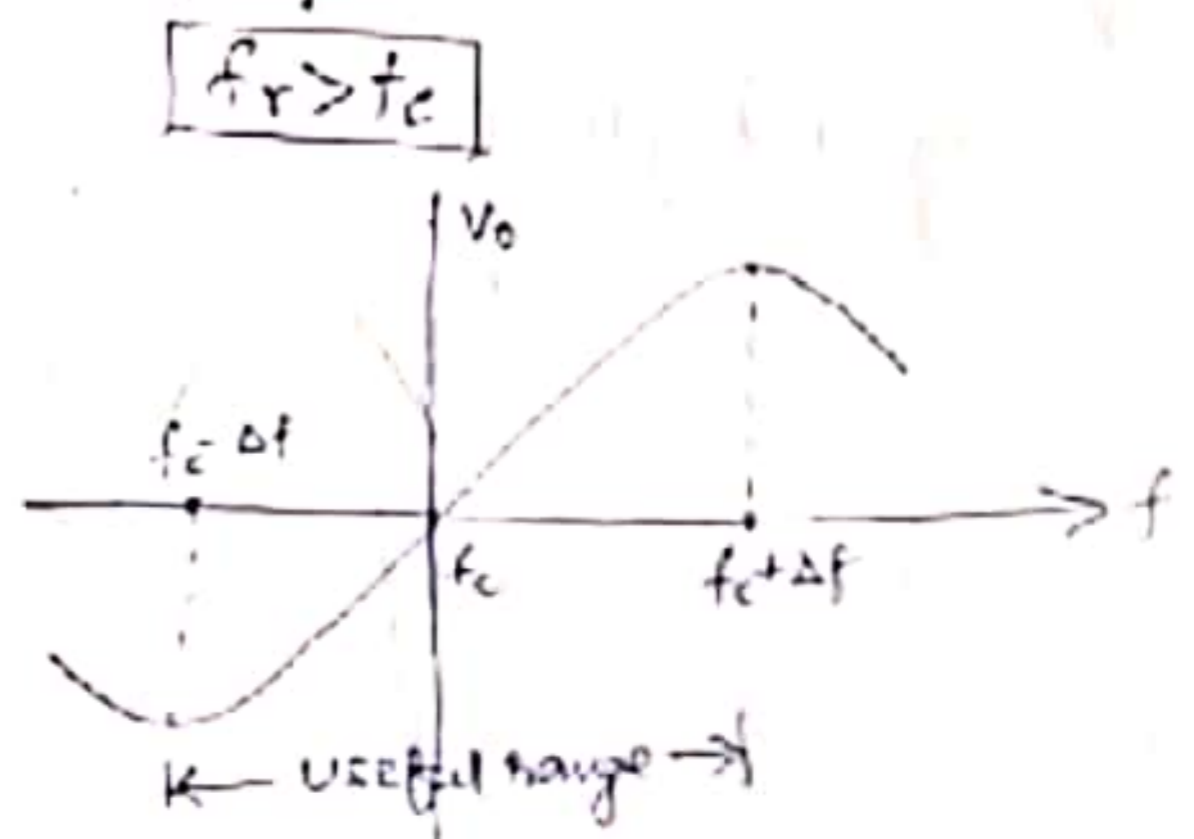
→ In slope detection a series RLC resonant ckt is used as freq selective n/w. The resonant freq of the RLC n/w is kept at  $(f_c + \Delta f)$ . The 3db point is kept at  $f_c$  &  $(f_c - \Delta f)$  is kept away from 3db point.



- Output of a tuned ckt depends on input freq. Since impedance of tuned ckt depends on input freq. So the output varies in accordance with the variation in input frequency.
- The resonance freq of tuned ckt ( $f_r$ ) is kept higher than the carrier freq ' $f_c$ '.

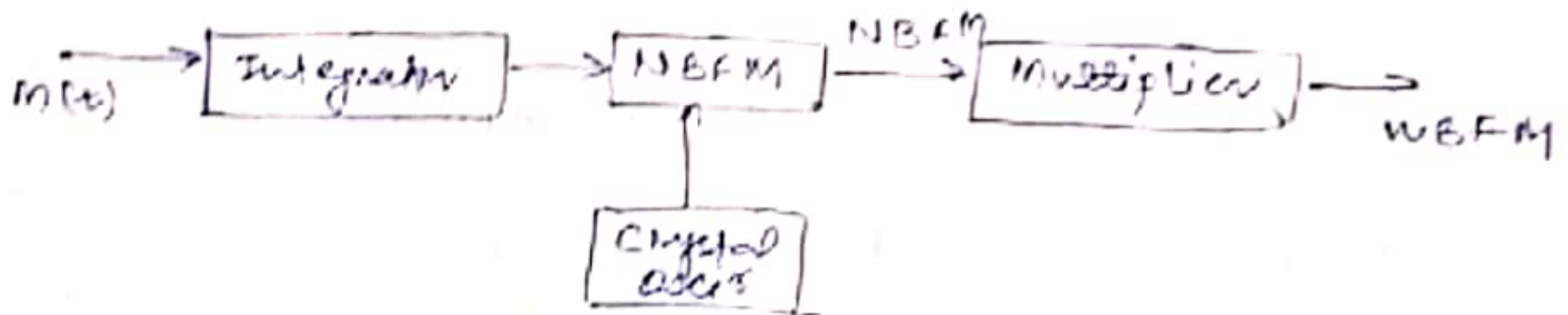


• Triple Tuned ckt



## Indirect method (Armstrong Method) of FM Generation

Most LC circ<sup>s</sup> are not stable enough to provide a carrier sig. The carrier sig usually vary due to temp. variations humidity and aging effect. So instead of using LC circ a crystal circ<sup>s</sup> must be use.



→ In this method the FM is obtained through phase modulation  
 → The operation of Armstrong method can be understood by dividing it into two parts as follows:

- Part 1 : Generating a narrow band FM using a phase modulator  
Part 2 : Using the Mixer and freq multipliers to obtain the desired values of freq deviation, modulation index and carrier.

$$X_{PM}(t) = A_c \cos[\omega_c t + \beta \sin \omega_m t]$$

$$= A_c \cos \omega_c t + \cos \beta \sin \omega_m t$$

$$= A_c \sin \omega_c t \sin \beta \sin \omega_m t$$

NBFM when  $\beta$  is very small

$$\left\{ \begin{array}{l} \cos \theta = 1 \\ \text{when } \theta \rightarrow 0 \end{array} \right.$$

$$\left. \begin{array}{l} \sin \theta = \theta \\ \text{when } \theta \rightarrow 0 \end{array} \right\}$$

$$\left. \begin{array}{l} \cos \beta \sin \omega_m t = 1 \\ \sin \beta \sin \omega_m t = \beta \sin \omega_m t \end{array} \right\} \Rightarrow \beta \rightarrow 0$$

$$X_{NBFM}(t) = A_c \cos \omega_c t - A_c \sin \omega_c t \beta \sin \omega_m t$$

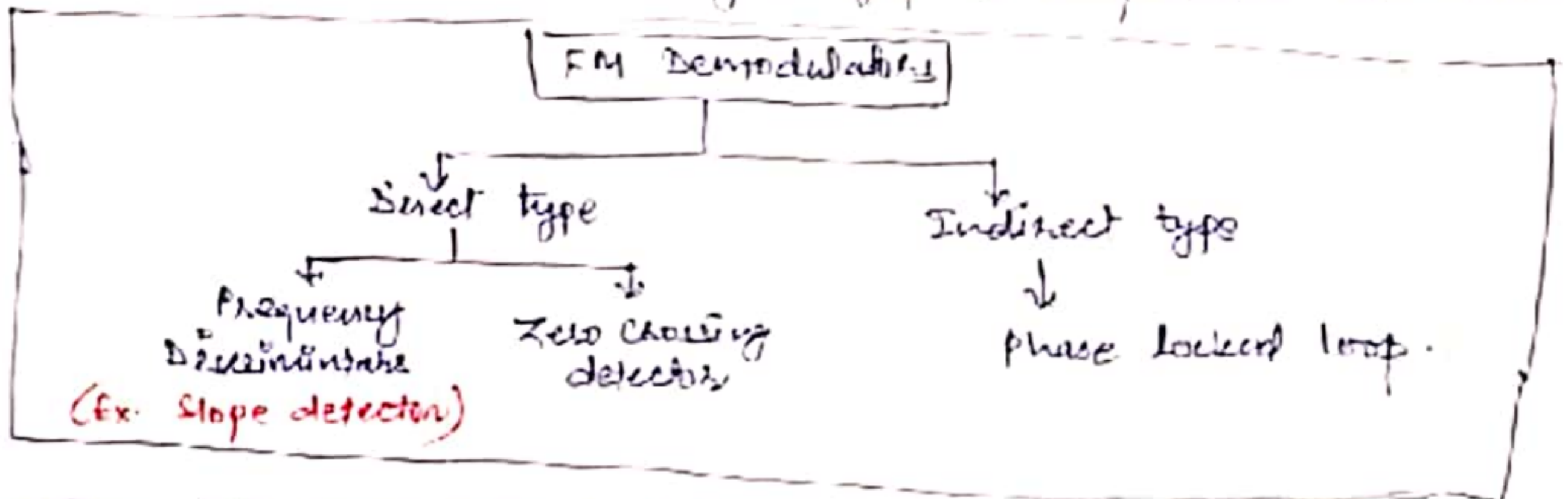
$$X_{NBFM}(t) = A_c \cos \omega_c t - \frac{A_c \beta}{2} [\cos(\omega_c - \omega_m)t - \cos(\omega_c + \omega_m)t]$$

$$= A_c \cos \omega_c t - \frac{A_c \beta}{2} \cos(\omega_c - \omega_m)t + \frac{A_c \beta}{2} \cos(\omega_c + \omega_m)t$$



## Demodulation of FM waves

- Frequency demodulation is the process that enables us to extract or recover the original modulating signal from frequency modulated wave.
- Demodulation of an FM wave requires a system that produces an output proportional to the instantaneous frequency deviations of the wave. This is called frequency discriminator.
- FM demodulator is basically a frequency to amplitude converter.



→ There are many ways to build FM demodulator but almost all of them are based on one of three principles.

- ① FM to AM conversion (Slope detector)
- ② Phase shift or quadrature detection (Foster Seeley)
- ③ Zero crossing detection

Let  $m(t) = A_m \cos \omega_m t$

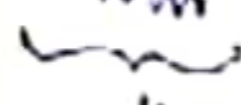
→ then in PM

$$\phi(t) = k_p m(t) = k_p A_m \cos \omega_m t$$



Modulation index  $\beta_{PM} = k_p A_m$

→ for FM,  $\phi(t) = k_f \int m(t) dt = k_f \int A_m \cos \omega_m t dt$   
 $= \frac{k_f A_m}{\omega_m} \sin \omega_m t$



Modulation index  $\beta_{FM} = \frac{k_f A_m}{\omega_m}$

So, 
$$\beta = \begin{cases} k_p A_m & \text{for PM} \\ \frac{k_f A_m}{\omega_m} & \text{for FM} \end{cases}$$

⇒ Modulation index or Max<sup>m</sup> value of phase deviation

Important points about  $\beta$

- In FM  $\beta$  decides the BW of FM.
- $\beta_{FM}$  can be greater than 1
- $\beta$  also decides no. of side bands having significant amplitude

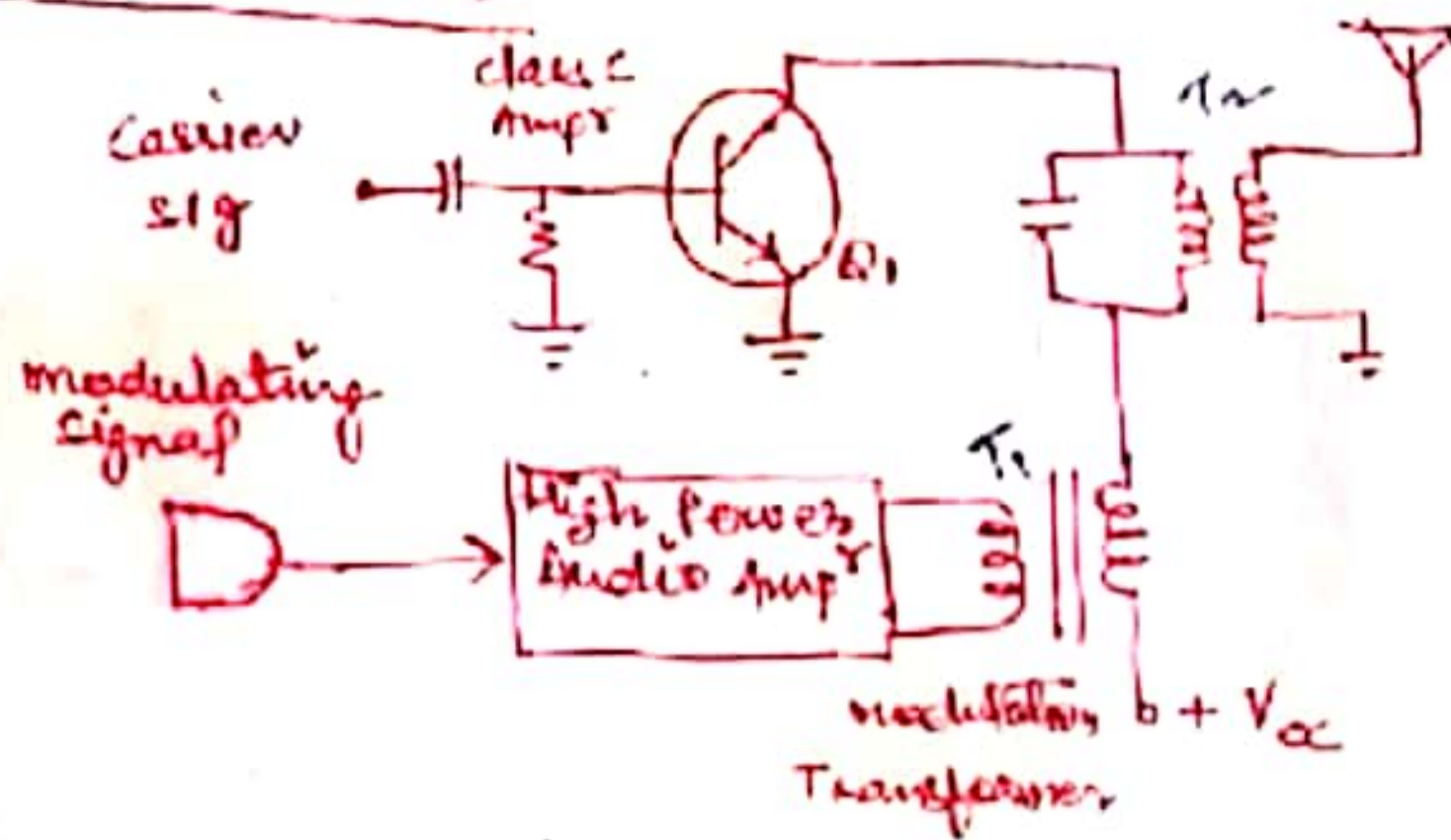
Deviation Ratio

→ The modulation index corresponding to the max deviation and max freq is called as deviation ratio.

$$D = \frac{\text{Max}^m \text{ deviation}}{\text{Max}^m \text{ modulating freq.}} = \frac{\Delta \omega}{\omega_m}$$

$D = \frac{\Delta \omega}{\omega_m}$

## Collector Modulator



- The modulator is a linear power Amp<sup>r</sup> that takes the low level modulating signal and amplifies it to a high power level. The modulating signal is coupled through modulation TF T<sub>1</sub> to the class C Amp<sup>r</sup>. The secondary winding of the modulation TF is connected in series with the collector supply voltage V<sub>cc</sub> of the class C Amp<sup>r</sup>.
- With zero modulation input signal, there will be zero modulation voltage across the secondary of T<sub>1</sub>. Therefore, the collector supply voltage will be applied directly to the class C Amp<sup>r</sup> and the carrier will be a steady sine wave.
- When the modulation signal occurs, the AC voltage across the secondary of the modulation TF will be added to and subtracted from the collector supply voltage.
- This varying supply voltage is applied to the class C Amp<sup>r</sup>. Naturally, the amplitude of the current pulses through transistor Q<sub>1</sub> will vary.
- As a result, the amplitude of the carrier sine wave varies in accordance with the modulated signal. For example, when the modulating signal goes positive, it adds to the collector supply voltage, thereby increasing its value and causing higher current pulses and a higher amplitude carrier. When the modulating signal goes negative, it subtracts from the collector supply voltage making it less. For that reason, the class C amp's current pulses are smaller, thereby causing a lower amplitude carrier signal.
- Hence amplitude modulated wave is obtained which is then transmitted through antenna.

## Angle Modulation

→ Angle mod<sup>n</sup> is a modulation in which the angle of a sine wave carrier is varied in accordance with the inf<sup>n</sup> contained in the modulating sig. while amplitude is const.

$$S_o(t) = A_c \cos[\omega_c t + \phi(t)]$$

↪ is a f<sup>n</sup> of msg sig

→ Angle Mod<sup>n</sup>  $\left\{ \begin{array}{l} \rightarrow \text{FM (Freq. of carrier is varied)} \\ \rightarrow \text{PM (Phase angle of carrier is varied)} \end{array} \right.$

→ Angle Mod<sup>n</sup> is being used for:

- ① Cellular radio
- ② Radio broadcasting
- ③ Satellite comm<sup>n</sup>
- ④ Microwave comm<sup>n</sup>
- ⑤ TV sound trans<sup>n</sup>

→ For Angle mod<sup>n</sup>  $S_o(t) = A_c \cos \theta(t)$

where  $\theta(t) = \omega_c t + \phi(t)$

$\phi(t) \rightarrow$  Instantaneous phase deviation

$$\omega_i = \frac{d}{dt} \theta(t) = \omega_c + \frac{d}{dt} \phi(t)$$

$\frac{d}{dt} \phi(t) \rightarrow$  Instantaneous freq deviation

## Demodulation of FM waves

- Frequency demodulation is the process that enables us to extract or recover the original modulating signal  $[m(t)]$  from frequency modulated wave.
- Demodulation of an FM wave requires a system that produces an output proportional to the instantaneous freq. deviation of the input signal. Such a system is called freq. discriminator.
- The FM demodulator operates on an altogether different principle than the AM detector. AM detector is basically a rectifier. But FM demodulator is basically a freq to amplitude converter.
- There are many ways to build FM demodulator, but almost all of them are based on one of three principles -

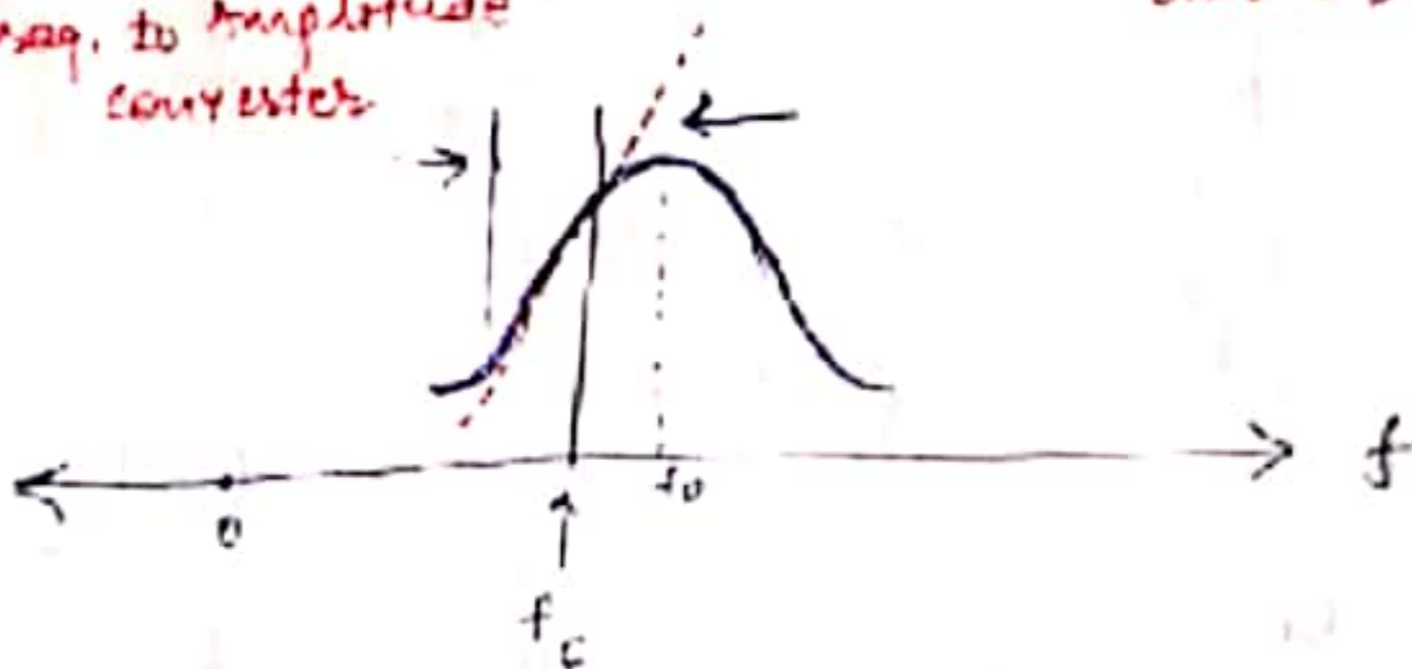
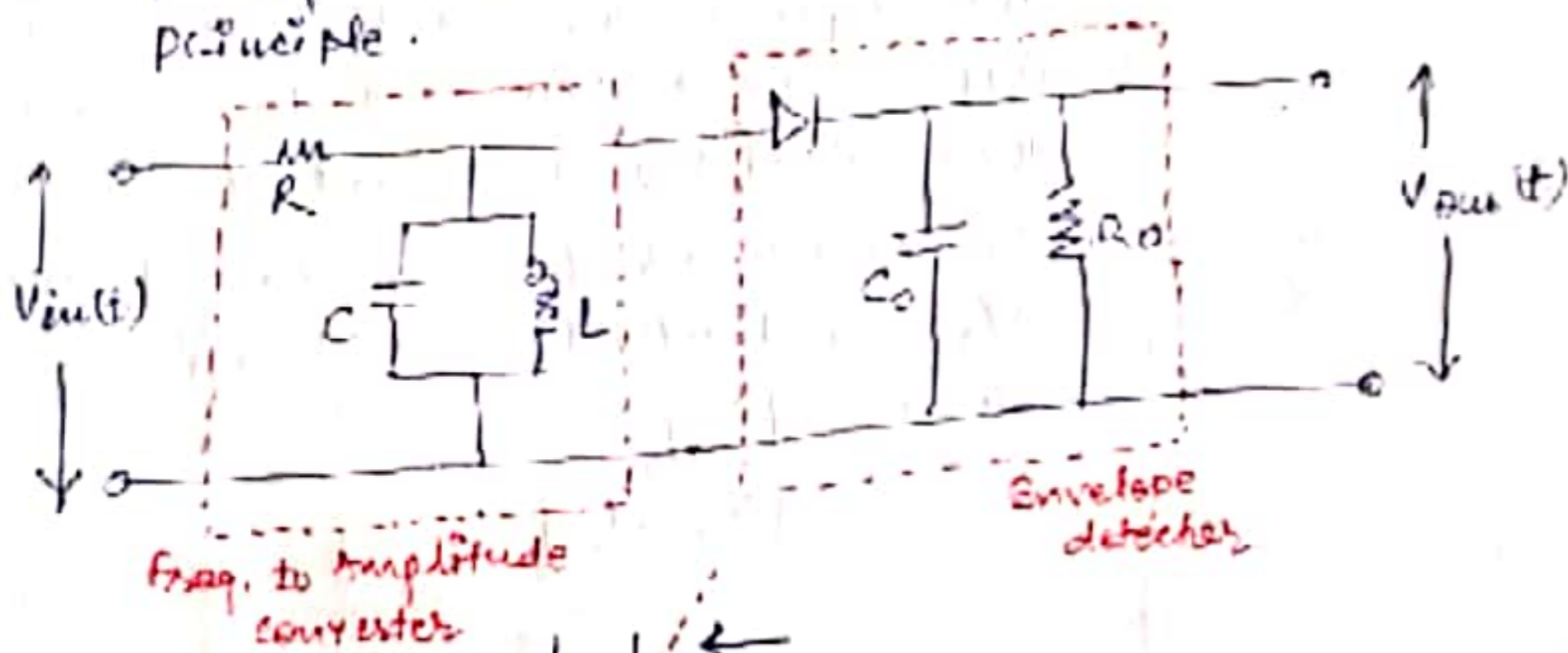
① FM to AM conversion Ex: slope detector

② Phase shift or quadrature detection

③ Zero crossing detection

## Slope detection

- A slope detector is an example of the FM to AM conversion principle.



## Phase Modulation

→ Phase mod<sup>n</sup> is a form of modulation that represents m as variations in the instantaneous phase of a carrier wave.  
Phase mod<sup>n</sup> is not very widely used for radio trans<sup>n</sup>.

→ In PM,

$$\phi(t) \propto m(t)$$

(Phase deviation is proportional to msg sig)

$$\phi(t) = k_p m(t)$$

Instantaneous phase deviation

Phase deviation const.

msg sig

→ So,

$$S_{PM}(t) = A_c \cos [\omega_c t + k_p m(t)]$$

$$\omega(t) = \omega_c + k_p \frac{d m(t)}{dt}$$

$$\omega_i = \frac{d \theta(t)}{dt} = \omega_c + k_p \frac{d m(t)}{dt}$$

\*\* } Thus in PM, the instantaneous freq  $\omega_i$  varies linearly with the derivative of msg sig.

Freq Modulation: FM conveys info over a carrier wave by varying its instantaneous freq. FM is widely used for broadcast of music and speech and in two way radio systems.

→ In FM, the instantaneous freq deviation  $\frac{d \phi(t)}{dt}$  is proportional to msg sig. i.e.

$$\frac{d \phi(t)}{dt} \propto m(t)$$

$$\frac{d \phi(t)}{dt} = k_f m(t)$$

$$\Rightarrow \phi(t) = k_f \int_{t_0}^t m(t) dt$$

(freq deviation const.)

→ So,

$$S_{FM}(t) = A_c \cos [\omega_c t + k_f \int m(t) dt]$$

$$\theta(t) = \omega_c t + k_f \int m(t) dt$$

$$\omega_i = \frac{d \theta(t)}{dt} = \omega_c + k_f m(t)$$

Adv

- ① High sensitivity & selectivity
- ② High adjacent channel rejection
- ③ No variation in B.W.

Image signal and image signal rejection

→ Superhetrodyne receiver suffers from a major drawback known as image freq problem.  
 → Image signal is a signal whose freq. is <sup>as</sup> higher with  $f_o$  as the  $f_{ds}$  is smaller than  $2f_o$ .

If  $f_o \rightarrow$  local osc freq.  $f_{ds} \rightarrow$  desired signal freq.  
 $f_i \rightarrow$  intermediate freq.

the,  $f_o - f_{ds} = f_i$   $\Rightarrow$   $f_{ds}$  is lesser than  $2f_o$  with an amount  $f_i$

By definition of image signal  $f_{im} = f_o + f_i$   $\Rightarrow$   $f_{im} \rightarrow$  image freq.

$$= f_i + f_{ds} + f_i$$

$$= f_{ds} + 2f_i$$

$\rightarrow$  from this eqn it is clear that image signal is  $2f_i$  higher than with desired signal

\* If this signal is reached to antenna mixer by antenna then it will produce same intermediate freq  $f_i$  which will be produced by desired signal  $f_{ds}$ .

$f_i = f_o - f_{ds}$

If produced by  $f_{ds}$

$f_i = f_{im} - f_o$

If produced by image freq.

$f_i = f_{im} - f_o$

$$= f_{ds} + 2f_i - f_o = f_{ds} + 2(f_o - f_{ds}) - f_o$$

$$= f_{ds} + 2f_o - 2f_{ds} - f_o$$

$$= f_o - f_{ds} \quad \text{--- (1)}$$

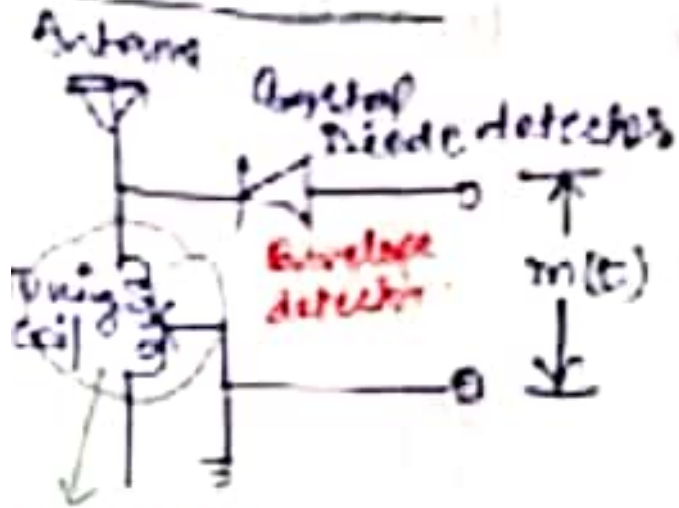
Acc to eqn (1) & eqn (2) desired signal and image signal produce same IF which will further amplify by IF amp and interfere with the signal. so the image signal must be rejected. which depends on selectivity

$\alpha = \sqrt{1 + Q^2 r^2} \Rightarrow$  Image freq. rejection ratio where  $r = \frac{f_{im} - f_{ds}}{f_{ds} - f_{im}}$

## Types of Radio Receiver

- ① Crystal radio Rx
- ② Tuned radio freq. Rx
- ③ Super heterodyne radio Rx

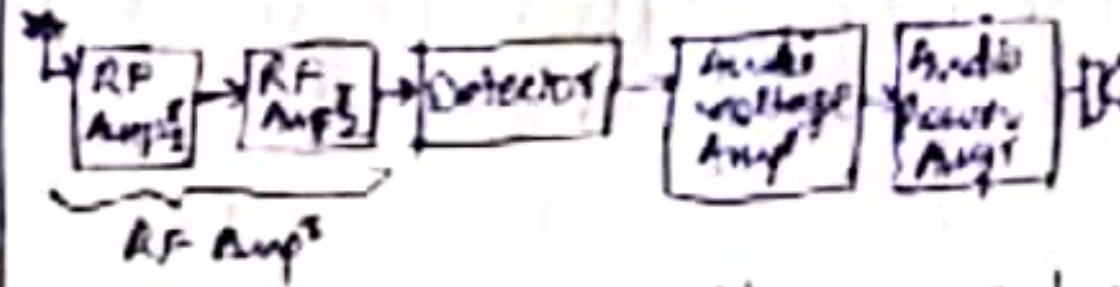
### Crystal Rx



Defined freq can be selected by changing turns of coil

- Selectivity & sensitivity is very poor
- Amp is not used so weak demodulated signal

### TRF Rx

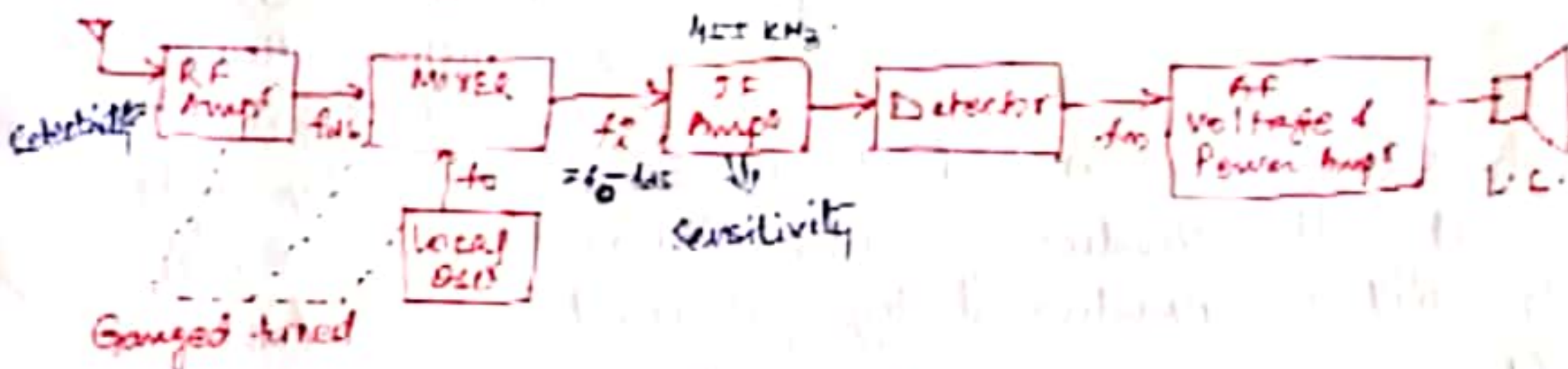


- Good only for medium wave freq but poor performance at higher freq.
- Intractable due to multiple RF amps, variation in B.W. Poor selectivity
- Simple circ & good sensitivity.

### SHRR

A superheterodyne Rx, often shortened to Superhet, is a type of Radio Rx that uses freq. mixing to convert a received signal to a fixed intermediate freq which can be more conveniently processed than the original carrier freq.

## Super Heterodyne radio Receiver.



$$f_0 = f_c + f_i$$

$$f_i = f_0 - f_c \rightarrow \text{is selected}$$

### Working

- The received signal is amplified by rf amp which is a tuned Amp. Amplified signal is passed on to a mixer. here of carrier is mixed with  $f_0$  generated by local osc. The process of mixing is called heterodyning.  $f_0$  is selected to be above  $f_c$ .
- Mixer generates sum and difference of freq ( $f_0 + f_c$ ) and ( $f_0 - f_c$ ). ( $f_0 + f_c$ ) eliminated by a filter. The difference freq ( $f_0 - f_c$ ) is called intermediate freq carrier.



## Operation

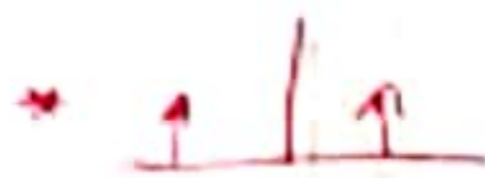
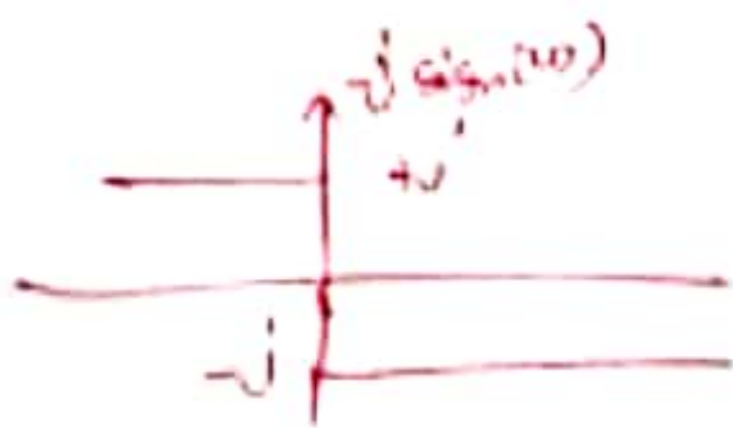
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In this way both forms of SSB waves can be generated.

- Hilbert TFA is the method of separating the sig. with respect to their phase contents & not with their freq.
- Hilbert transform separates the sig. with a phase diff. of  $90^\circ$  to them.

$$\begin{aligned}
 x(t) \rightarrow \text{sig} &\Rightarrow \hat{x}(t) = x(t) * \frac{1}{\pi t} \\
 &= \int_{-\infty}^{\infty} \frac{x(\tau)}{\pi(t-\tau)} d\tau \\
 \hat{X}(\omega) &= X(\omega) \cdot [-j \operatorname{sgn}(\omega)]
 \end{aligned}$$



$\Rightarrow$



## Comparison AM and Angle Mod<sup>n</sup>

Angle modulation has following advantages over AM

- ① The amplitude of FM is const. It is independent of depth of modulation. Hence Tx power remains constant in FM whereas it varies in AM.
- ② Since amplitude of FM is const., the noise interference is minimum in FM. Any noise superimposed on amplitude can be removed with the help of amplitude limits, whereas it is difficult to remove amplitude variations due to noise in AM.
- ③ The depth of modulation has limitation in AM. But in FM the depth of modulation can be increased to any value by increasing the deviation, this does not cause any distortion in FM sig.
- ④ Since guard bands are provided in FM, there is less probability of adjacent channel interference.
- ⑤ Since space waves are used for FM, the radius of prop<sup>n</sup> is limited to line of sight. Hence it is possible to operate several independent Tx on same freq with min<sup>m</sup> interference.
- ⑥ Since FM uses VHF and UHF ranges, the noise interference is min<sup>m</sup> compared to AM which uses MF and HF ranges.

### Disadv:

- ① BW requirement is much higher than AM.
- ② The Tx transmitting & receiving equipment is more complex and costly.
- ③ Since FM uses VHF & UHF range of freq, its area of reception is limited only to line of sight. This is much lower than area covered by AM.